

A Simple Complex Phenomenon of Urban Parking

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Parking is a long lasting urban blight

- Cruising for parking is the last leg of the car-based trip
- Cruising is linked to many urban externalities:
 - Congestion, air pollution and noise, loss of space, social inequity
- Parking has mostly been left to engineers to solve supply/operational issues by building lots

Cruising for parking may reach 30% of urban traffic in the city centers



Common belief, attributed to Donald Shoup: To avoid cruising we need 15% (1 of 7) of parking spots to remain free all the time

Deterministic model of cruising for parking

Parameters


Arrivals

 a cars/min

Departure rate

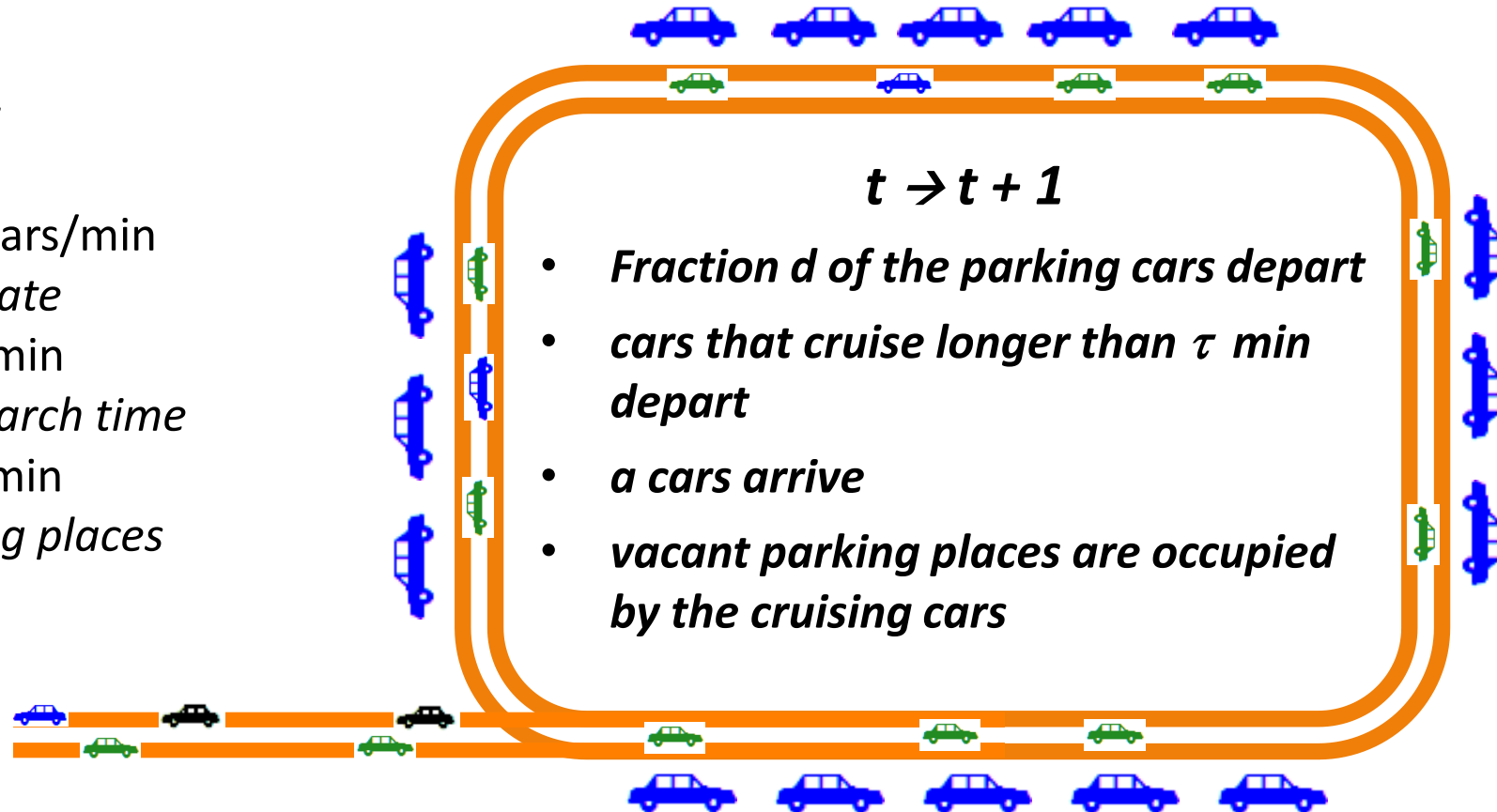
 d /min

Maximal search time

 τ min

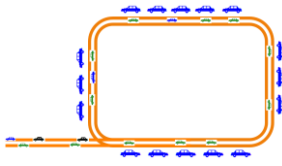
Total parking places

R



Initial conditions: All parking places are occupied

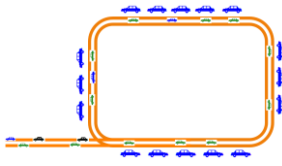
Deterministic model of cruising for parking



- State of the system $\mathbf{M}(t) = \langle M_0(t), M_1(t), \dots, M_{\tau-1}(t) \rangle$,
 $M_\mu(t)$ is the numbers of cars cruising for μ minutes
- Total number of cruising cars $N(t) = M_0(t) + M_1(t) + \dots + M_{\tau-1}(t)$
- $O(t)$ – Number of occupied parking places
- $F(t)$ - Cars that failed to find a parking place
- $p(t)$ - probability to park

$$p(t) = \min\{1, [\text{number of free places}]/[\text{number of cruising cars}]\}$$

Deterministic model of cruising for parking



Parameters


Arrivals

 a cars/min

Departure rate

 d /min

Maximal search time

 τ min

Total parking places

R

$O(t)$ – Number of occupied parking places

$F(t)$ - Cars that failed to find a parking place

$p(t)$ - probability to park

The dynamics of $M(t)$, $O(t)$ and $F(t)$:

$$M_0(t + 1) = a$$

$$M_1(t + 1) = M_0(t) * [1 - p(t)]$$

...

$$M_{\tau-1}(t + 1) = M_{\tau-2}(t) * [1 - p(t)]$$

$$F(t + 1) = F(t) + M_{\tau-1}(t) * [1 - p(t)]$$

$$O(t + 1) = \min\{(1 - d) * O(t) + N(t), R\}$$

Auxiliary equation to estimate parameters at t

$$N(t) = M_0(t) + M_1(t) + \dots + M_{\tau-2}(t) + M_{\tau-1}(t)$$

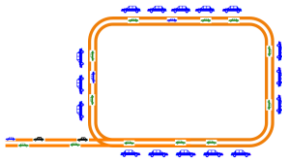
$$p(t) = \min\{1, f(\varepsilon, \mu)/N(t)\} \cong \min\{1, (R - (1 - d) * O(t))/N(t)\}$$

ε - average number of free places per link,

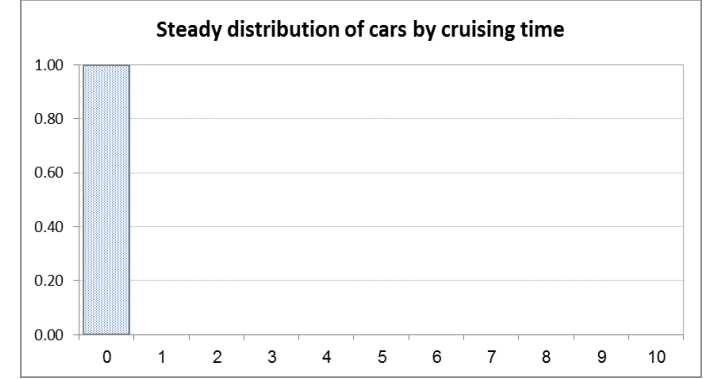
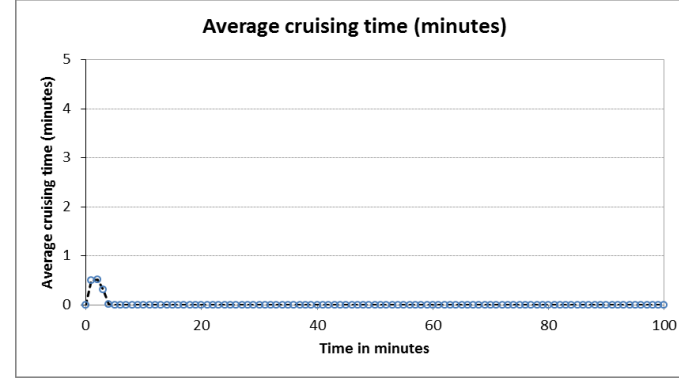
μ - average number of cruising cars per link

* N. Levy, K. Martens, I. Benenson, 2013, *Transportmetrica A*, 9 (9), 773–797

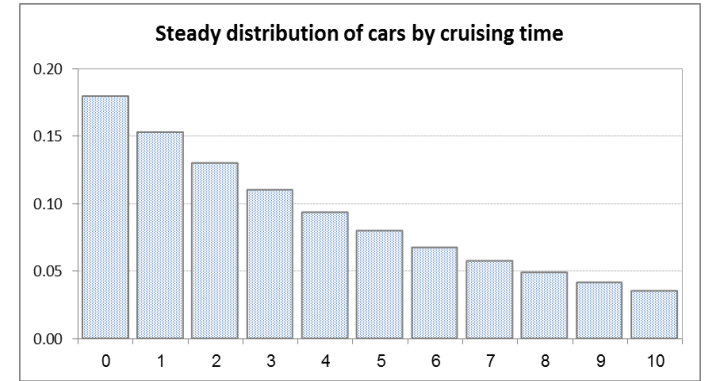
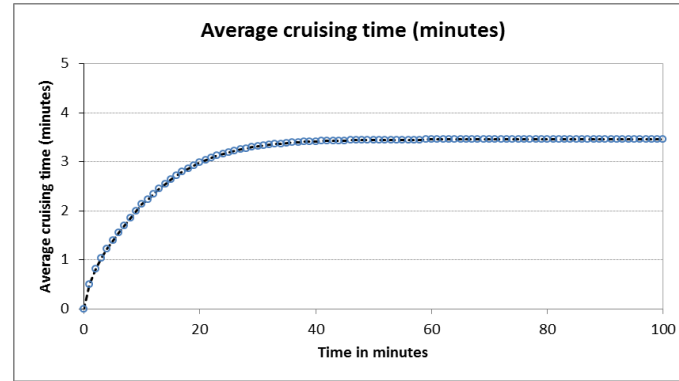
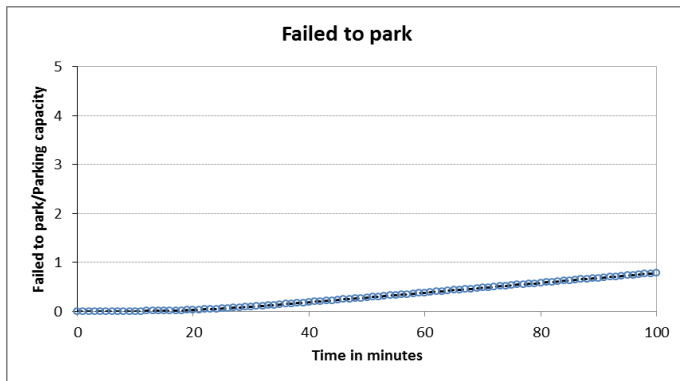
Deterministic model of cruising for parking



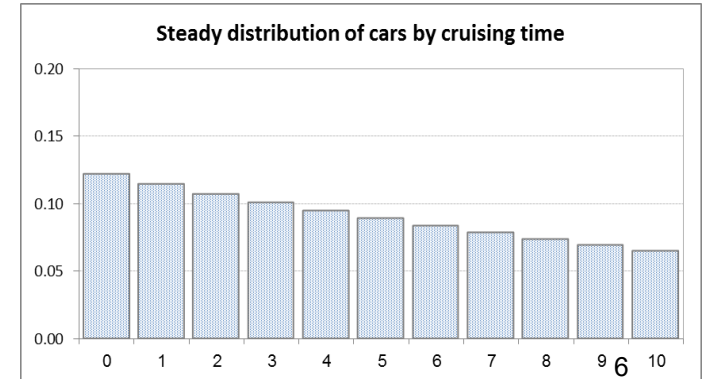
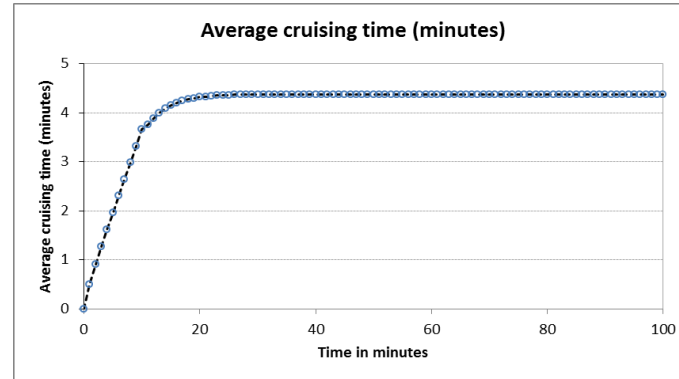
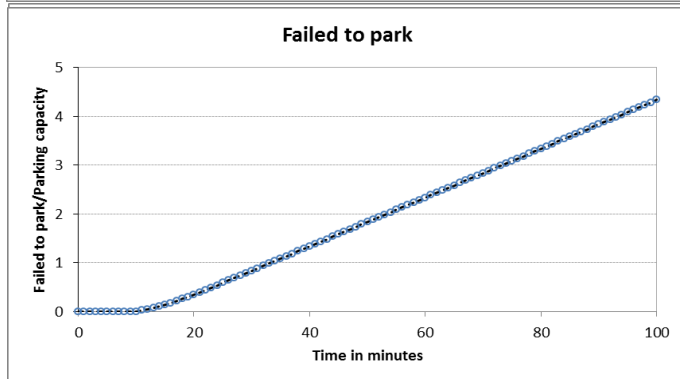
Arrivals: 4/min
Dep. rate: 0.05
Capacity: 100



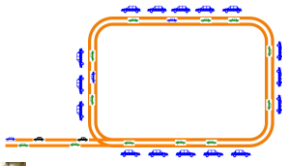
Arrivals: 6/min
Dep. rate: 0.05
Capacity: 100



Arrivals: 10/min
Dep. rate: 0.05
Capacity: 100



Deterministic model of cruising for parking: Conclusions



- Parking search is either easy or takes a long time
- Drivers' reaction or regulator's intervention may reduce the number of arriving cars and result in basic alteration of parking dynamics.

Parking reality: Spatio-Temporal Heterogeneity

Local aspects (driver's behavior, conditions at a destination)

- Parking demand, parking supply, and drivers' behavior are essentially heterogeneous, in space and in time
- They are defined by many factors: land-use, population, type (on/off-street) and location of parking, price, distance to destination, control



Global and long-term aspects (urban parking policy)

- Parking supply and, sometimes, demand, are defined by the city
- Drivers may be enforced to think of parking when planning a trip

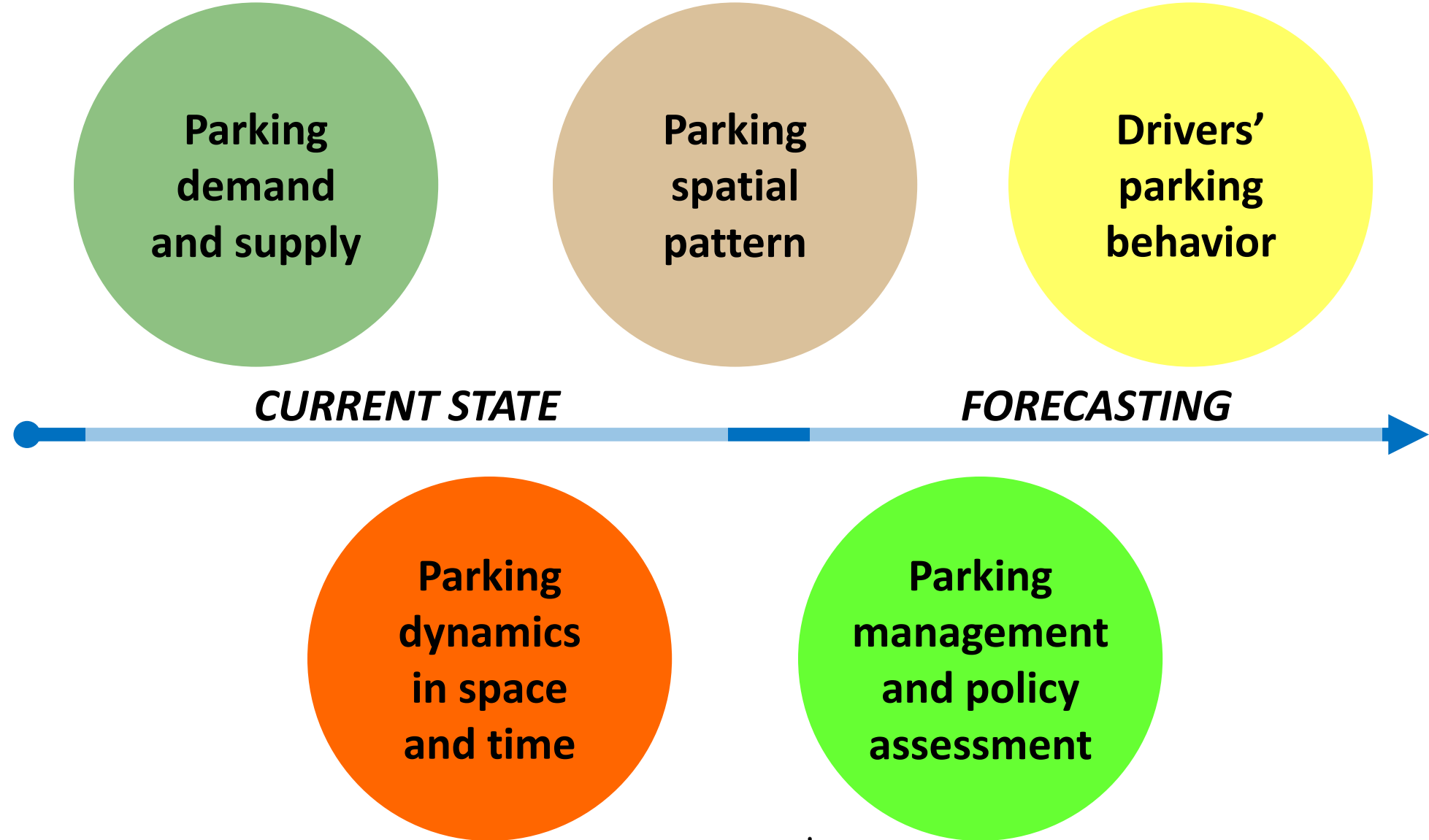


Parking planning (future transportation)

- What will be travelers' mode choice in the future?
- What is parking demand for the autonomous cars?



COMPONENTS OF PARKING REALITY



GIS + Aerial photos + Population Census

URBAN GIS, AERIAL PHOTOS



DEMAND

Night:

Households* (Car ownership rate)

Day:

Households' turnover + Office area/20 + Shops' turnover

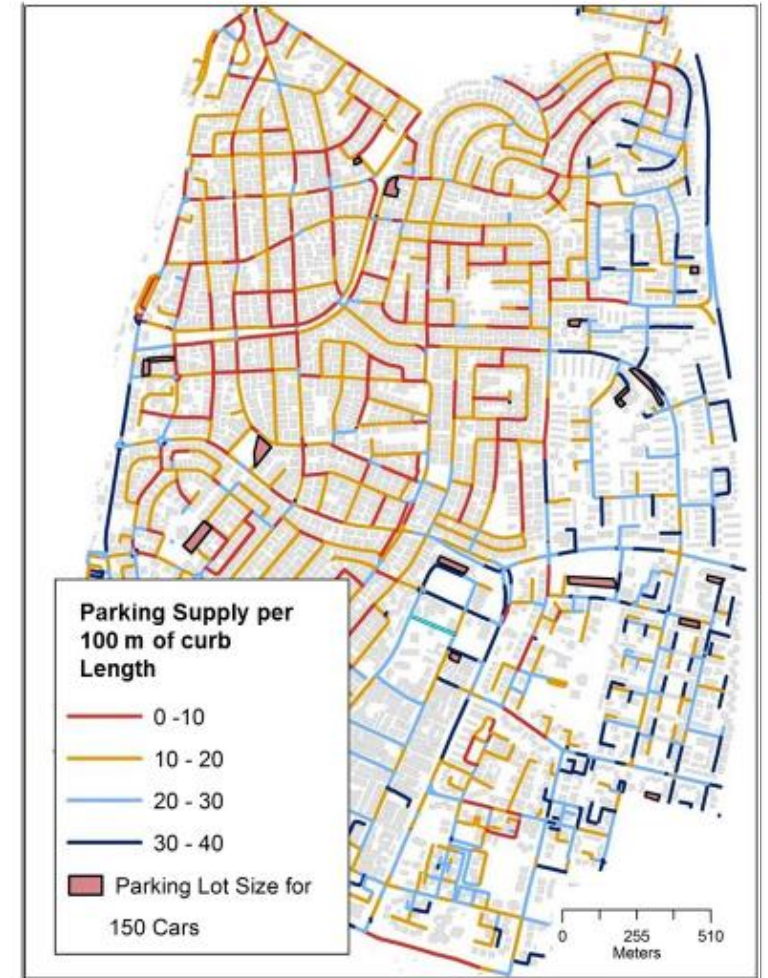
SUPPLY

Curb:

(Street length)/5 - Prohibited spots

Lots:

(Lot floor area)/12 (5*1.5 ~ 8m² car + 4m² pass)

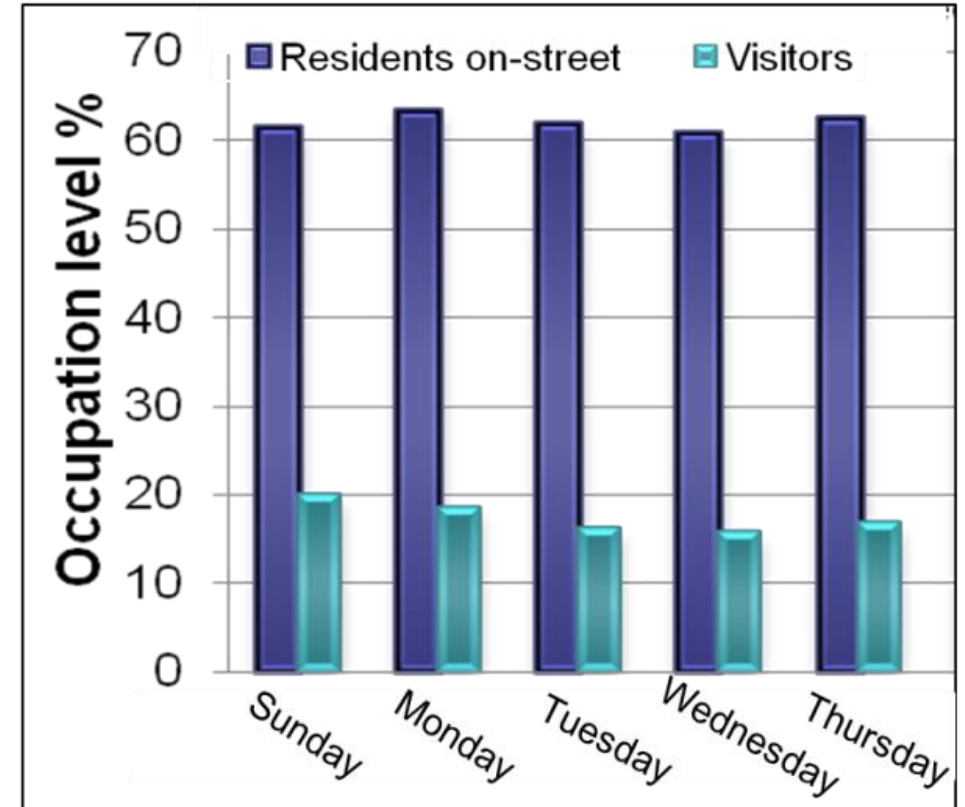


*Levy, N., Benenson, I, 2015, *Journal of Transport Geography*, 46, 220–231

Parking turnover: Field surveys in Basel neighborhood, TLV



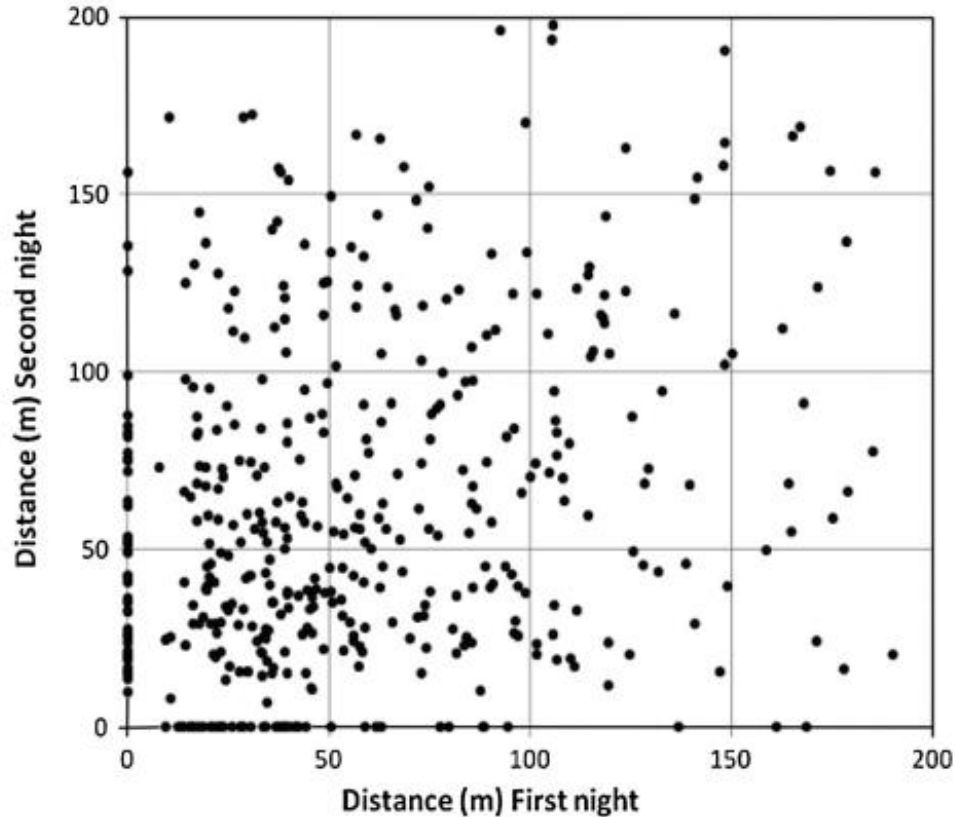
For the same day of the week and hour of the day: The variation in the parameters of parking pattern is very low



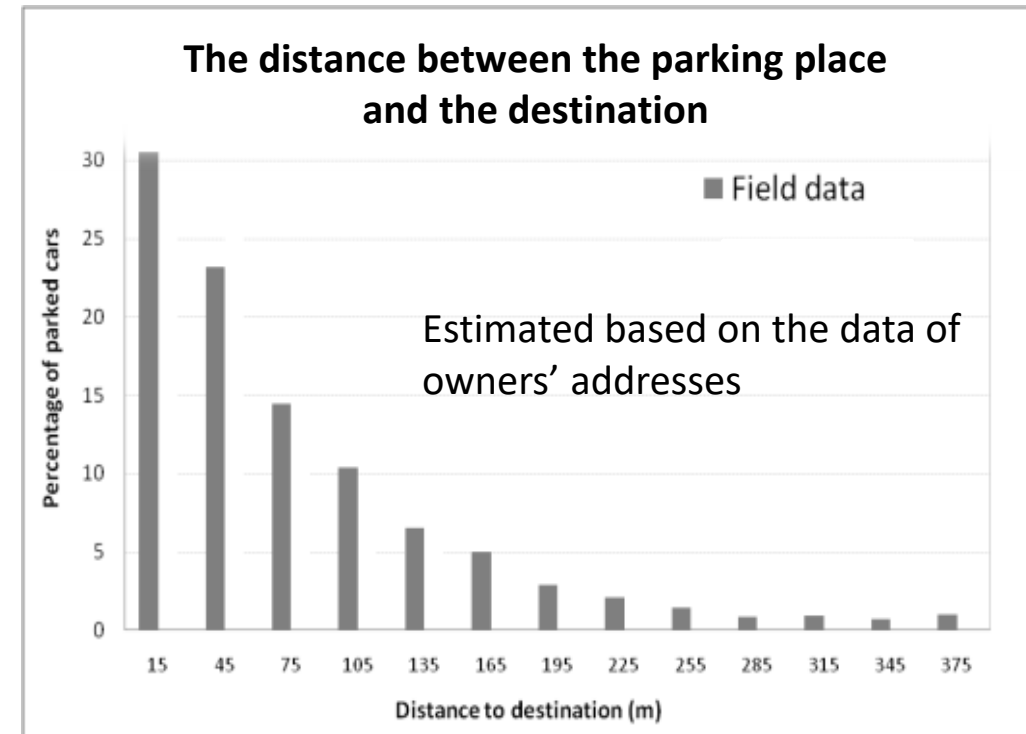
Residents		Visitors	
Average occupancy (weekdays)	STD	Average occupancy (weekdays)	STD
61.8%	0.94%	17.4%	1.77%

* N. Levy, K. Martens, I. Benenson, 2013, *Transportmetrica A*, 9 (9), 773–797

Destination-parking place distance: Field surveys in Basel neighborhood, TLV



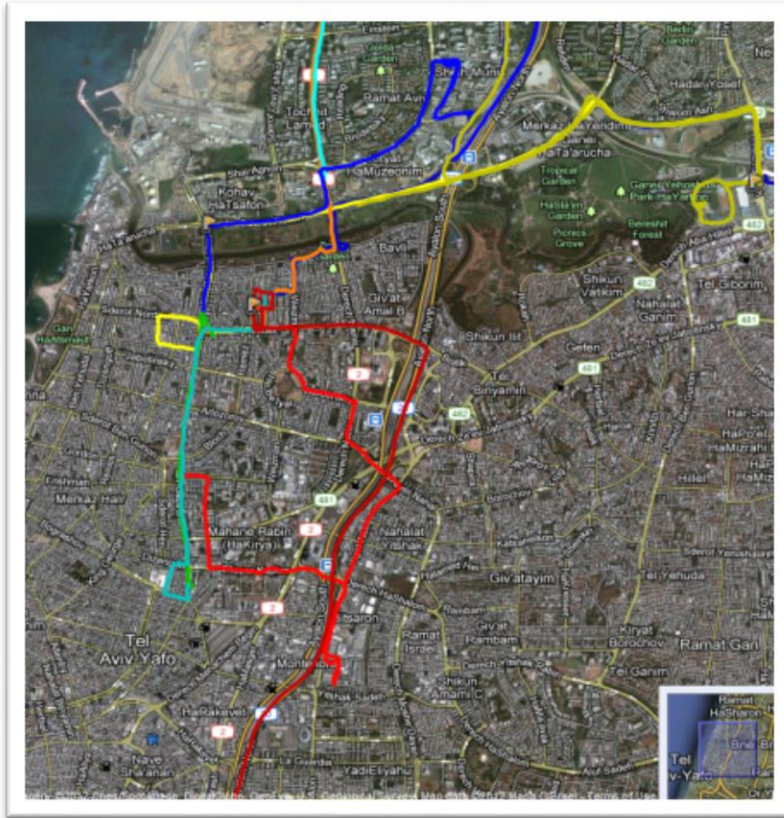
We possess reliable estimates of the parking demand, supply, spatial patterns, and turnover



*Levy, N., Benenson, I, 2015, *Journal of Transport Geography*, 46, 220–231

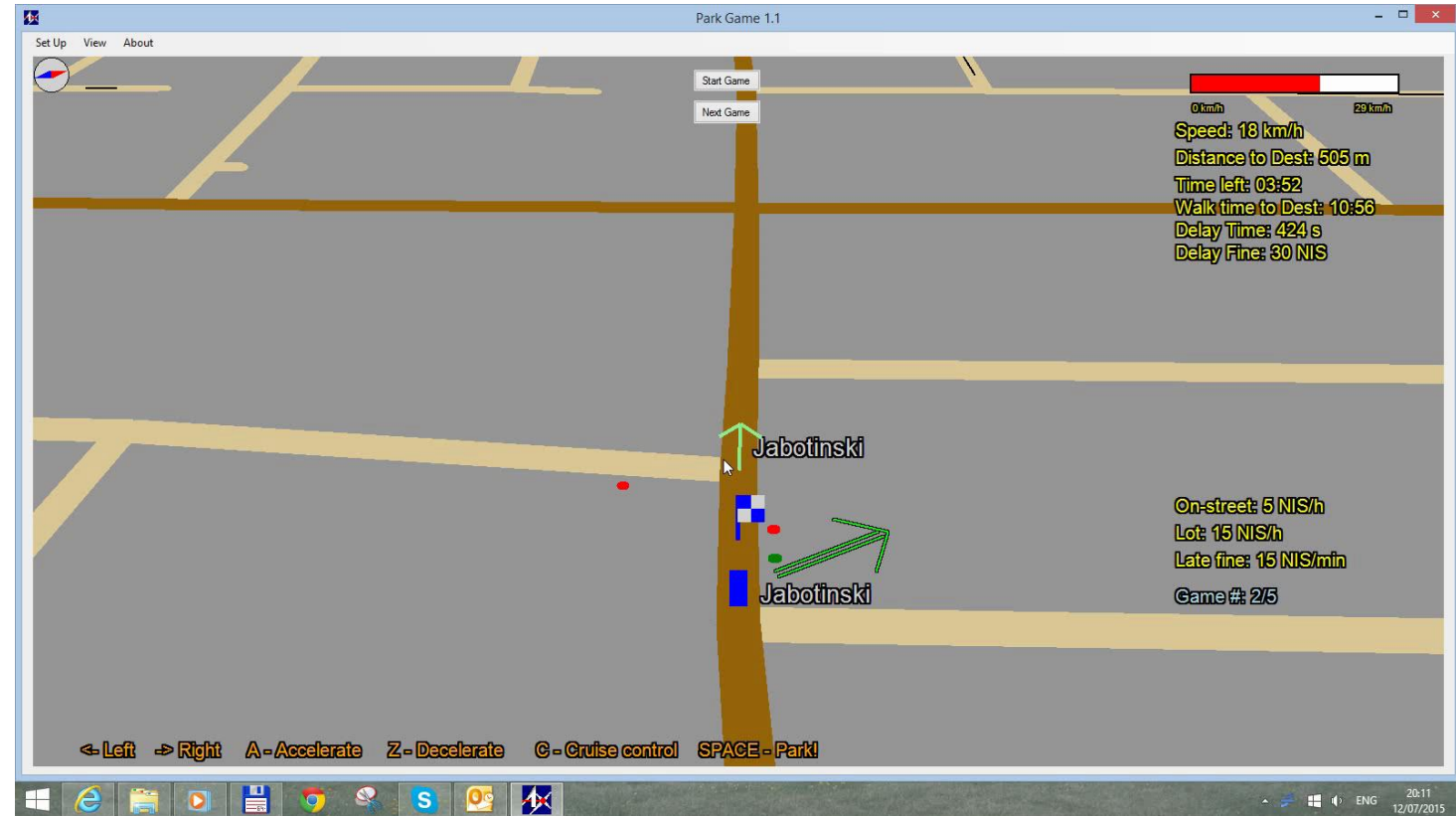
Drivers' parking search behavior

GPS logging, interviews



Driver's speed during parking search is 3 - 4 m/s (12-16 km/h)

ParkGame

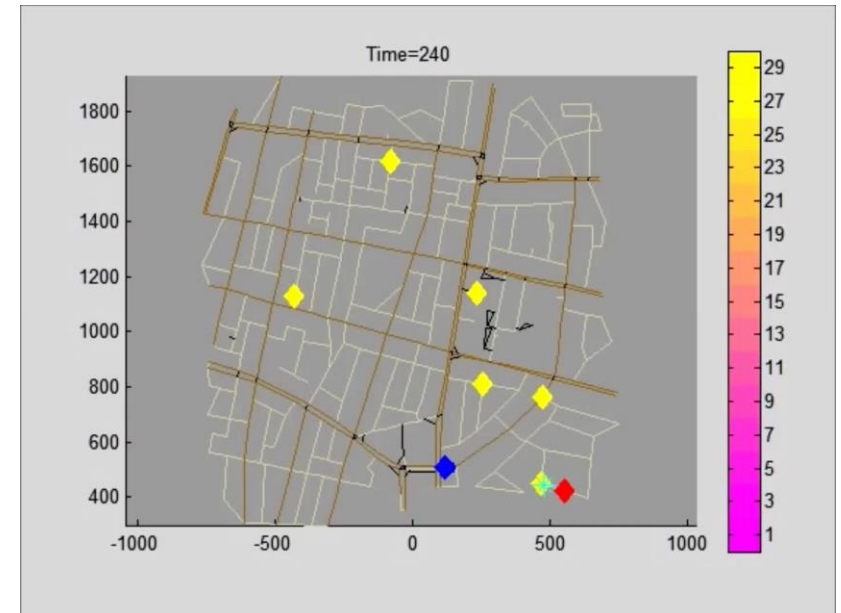
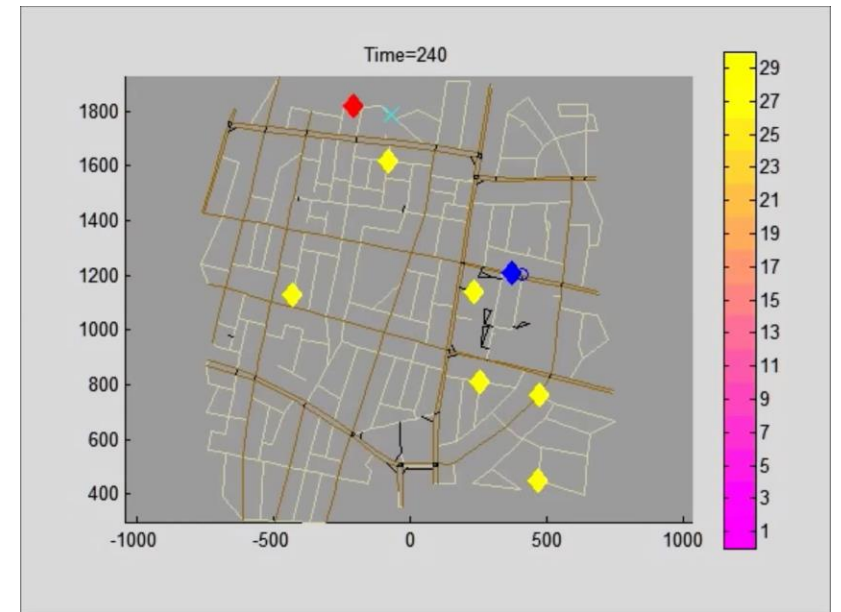


Understand cruising behaviour and the choice between curb and lot parking based on simulated cruising experience

ParkGame output

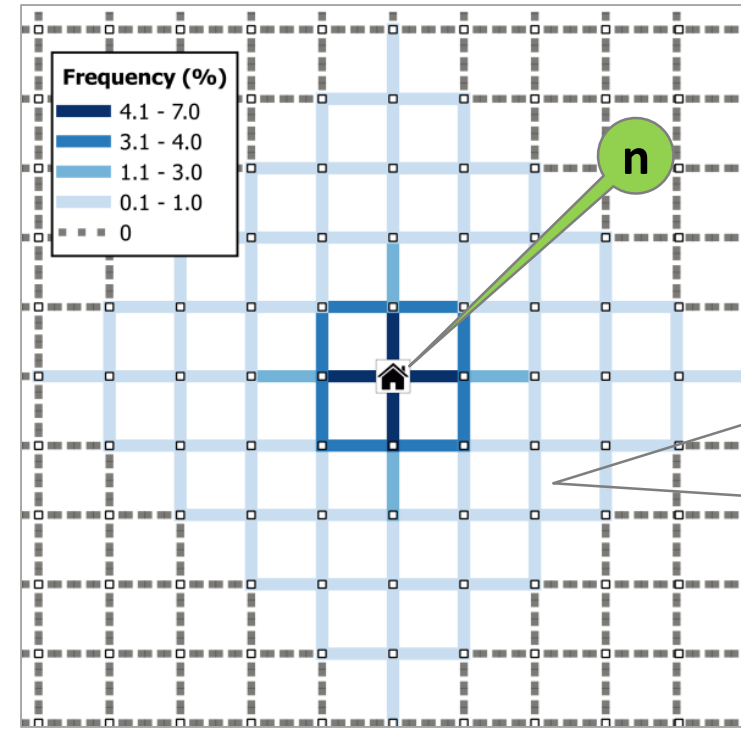
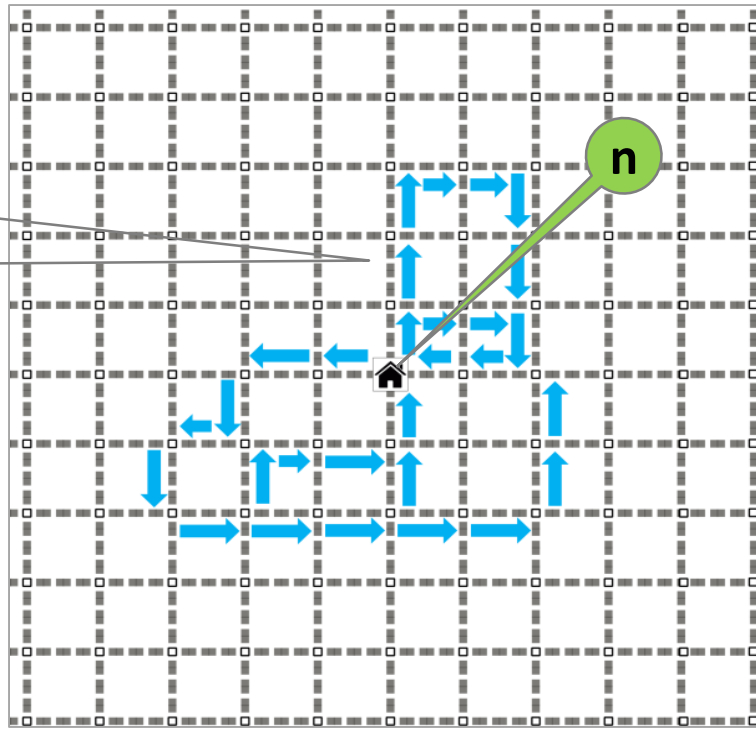
Driver's position and speed are recorded every second

Time	SegmentID	DistanceF	Free	Occupied	PType	Cruise Co	Dist. to D	Speed
240	1065280-1	0	0	3	0	OFF	428	14.4
239	1065280-1	0	0	3	0	OFF	428	14.4
238	1065280-1	0	0	3	0	OFF	428	14.4
237	1065280-1	0	0	3	0	OFF	428	14.4
236	1065280-1	0	0	3	0	OFF	428	14.4
235	1065280-1	1.28	0	3	0	OFF	429	14.4
234	1065280-1	2.56	0	3	0	OFF	430	14.4
233	1065280-1	3.52	0	3	0	OFF	431	14.4
232	1065280-1	4.8	0	3	0	OFF	433	14.6
231	1065280-1	6.13	0	3	0	OFF	434	15.8



ParkGame drivers' behaviour : Biased random walk

Typical cruising trajectory

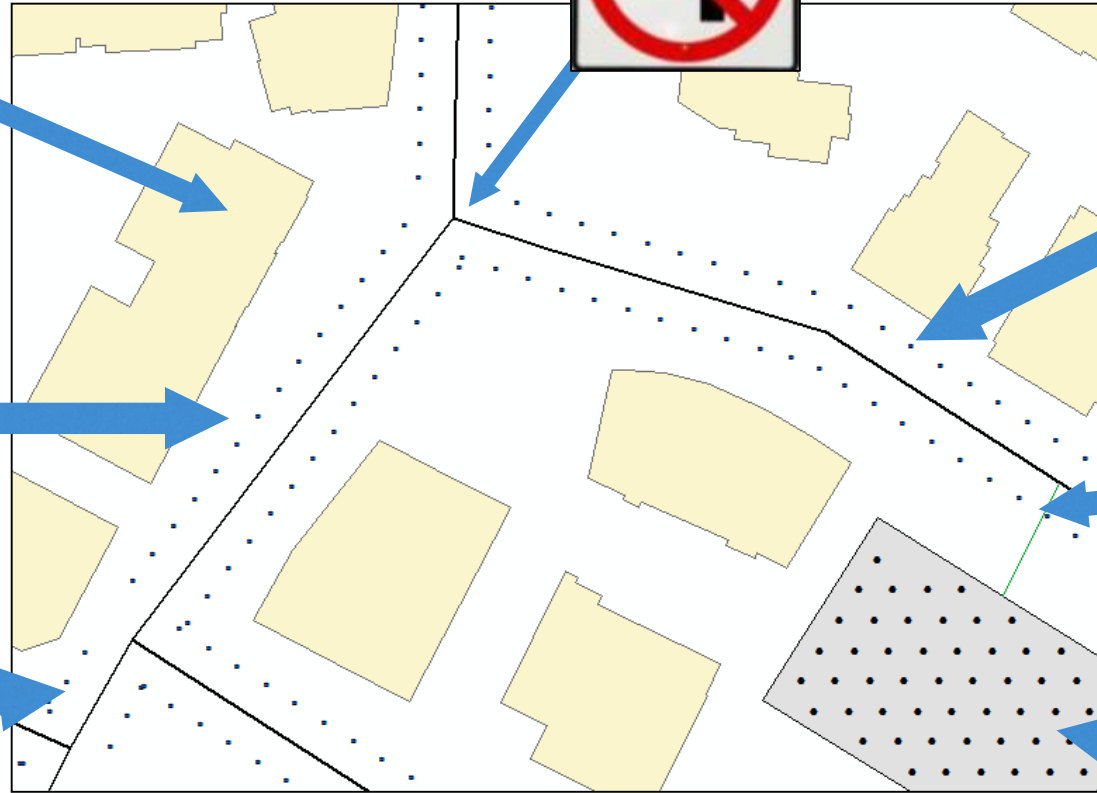
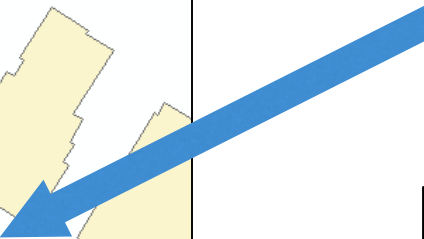
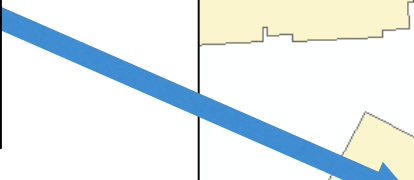


Probability $p_n(l)$ to visit a links when searching for parking near to a destination n

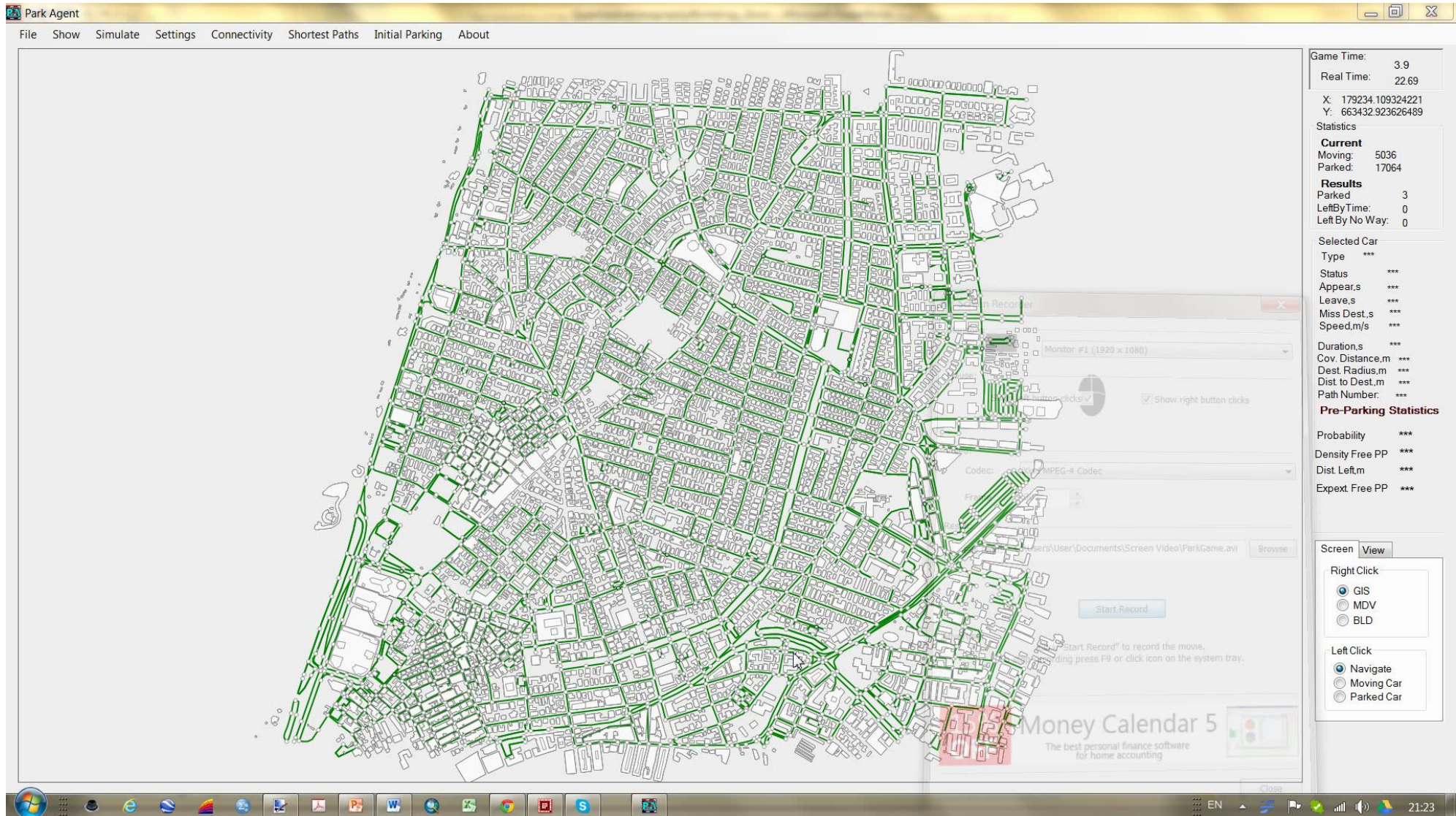
Driver's behavior parameters

Decision at a previous junction	$d < 100$		$100 \leq d < 200$		$200 \leq d < 300$		$d \leq 300 < 400$		$d \geq 400$	
	Closer	Further	Closer	Further	Closer	Further	Closer	Further	Closer	Further
Closer	0.00	1.00	0.65	0.35	0.85	0.15	0.90	0.10	1.00	Irrelevant
Further	Irrelevant		0.00	1.00	0.80	0.20	0.85	0.15	1.00	0.00

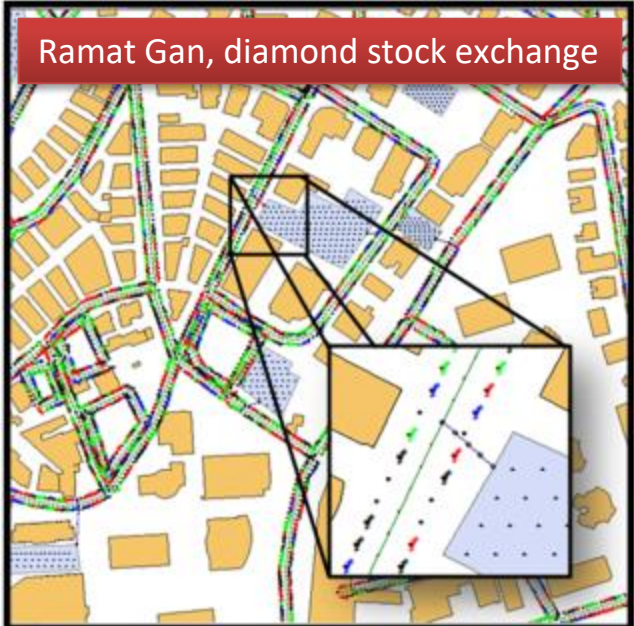
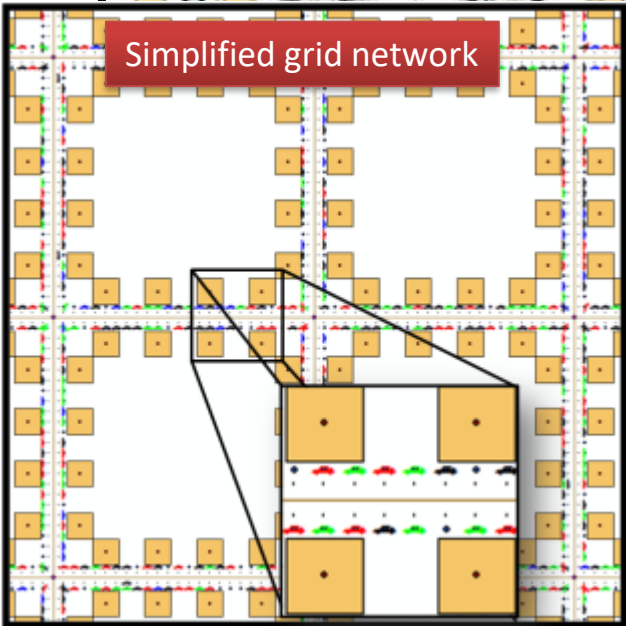
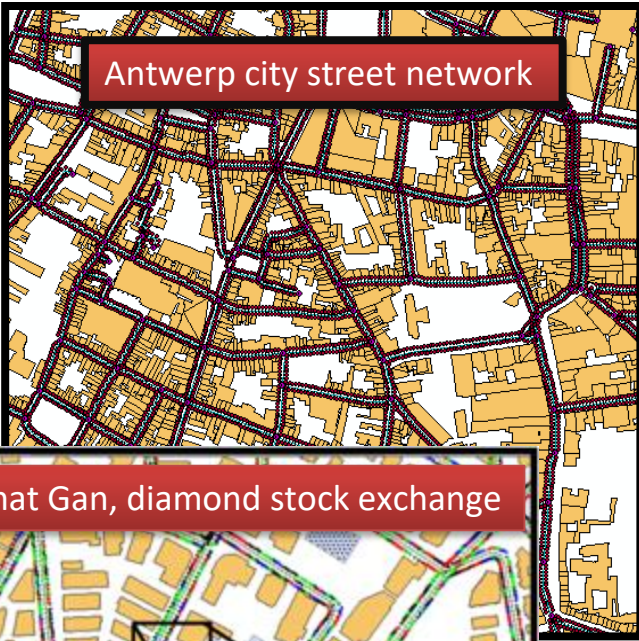
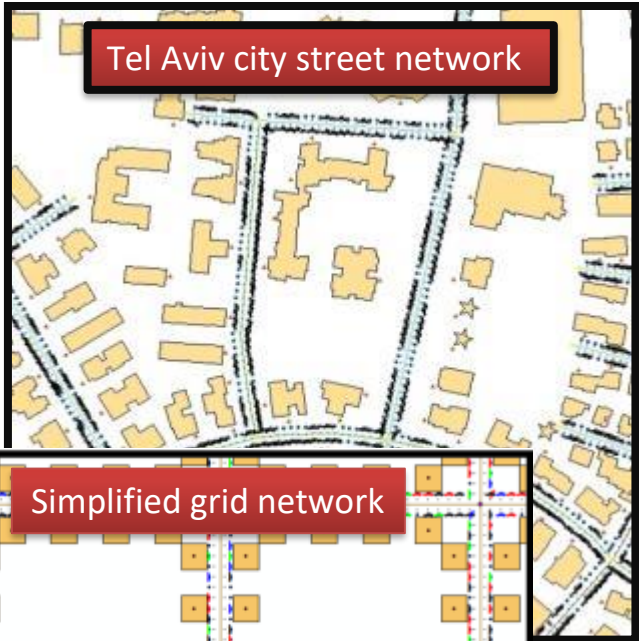
PARKAGENT - spatially explicit model of cruising for parking



PARKAGENT: User interface



PARKAGENT: Easily adjustable to a new city



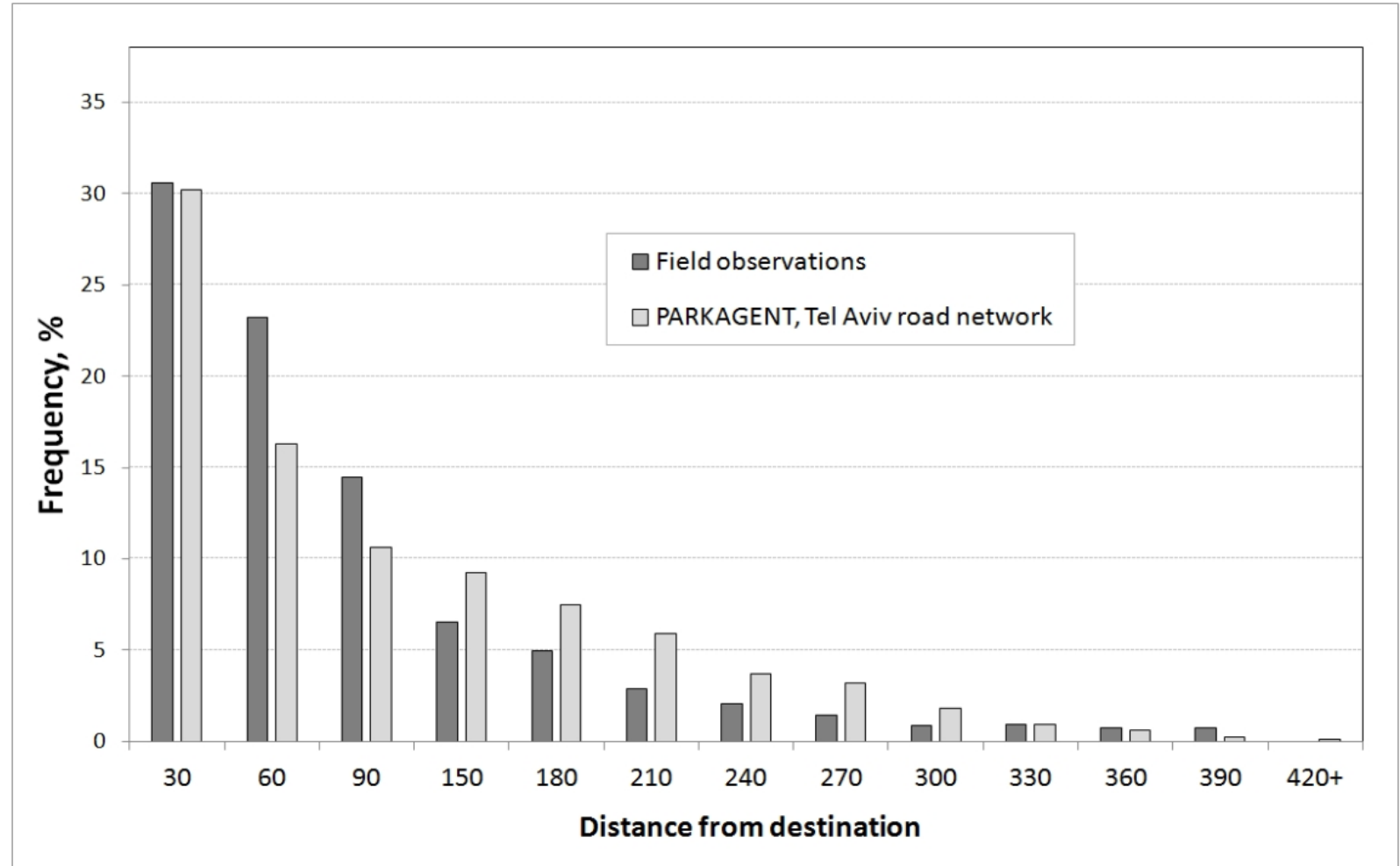
ParkAgent: Quantitative fit to the Tel Aviv data

Parameters

Parking demand:
Estimated based on
buildings' capacity

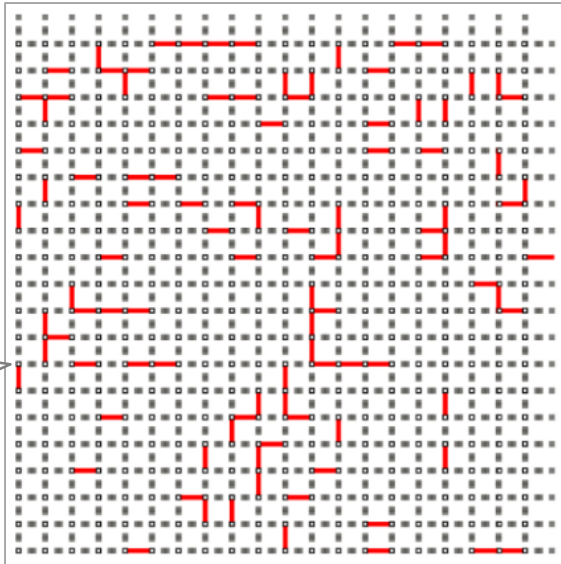
*Spots occupied
during the whole
day: 40 – 80%*

*Duration of visitors'
parking: Uniform,
[30 min, 120 min]*

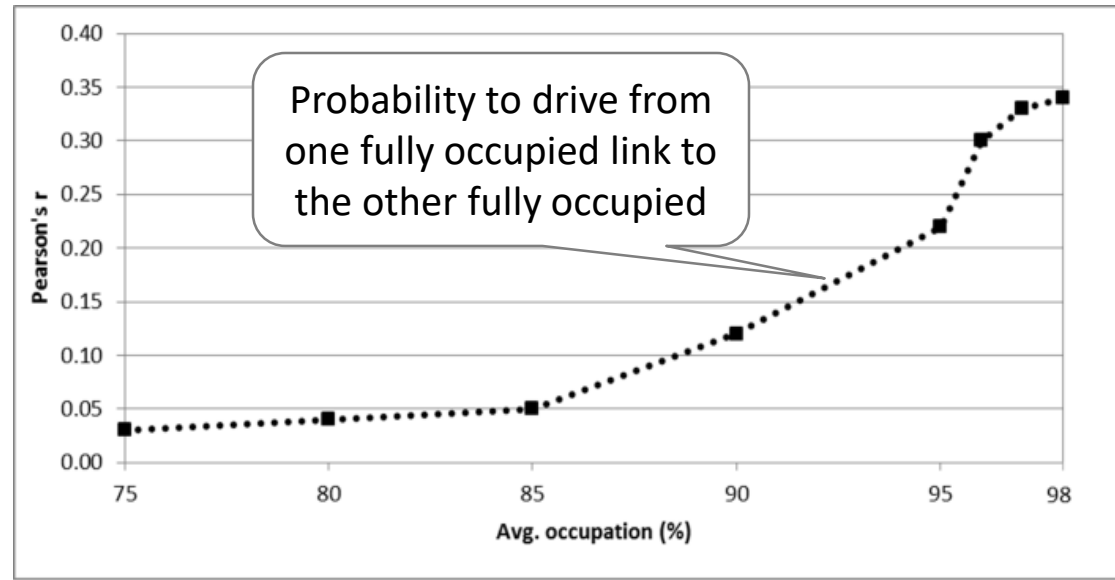
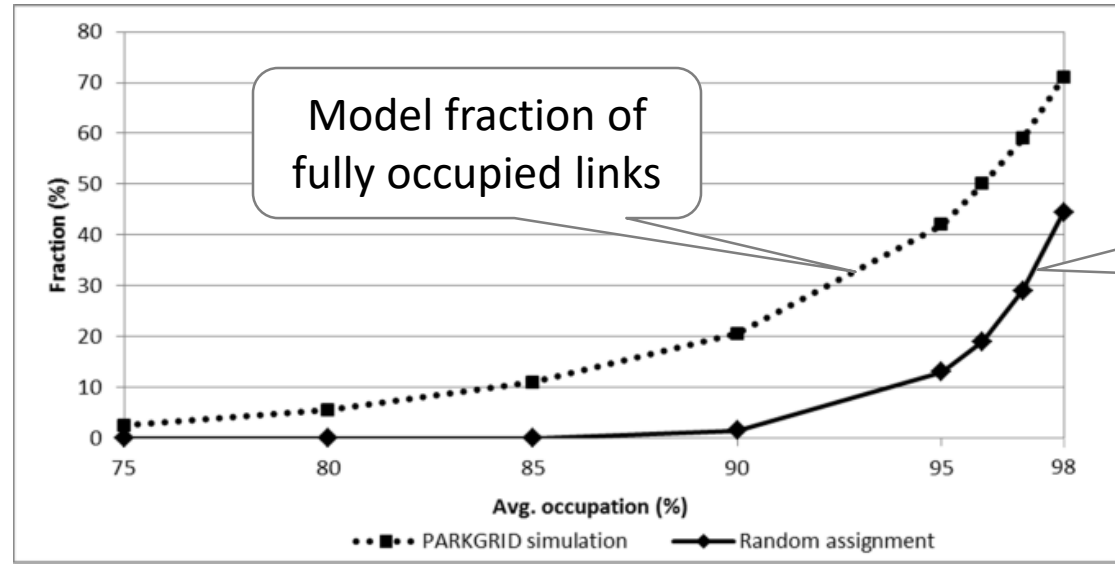
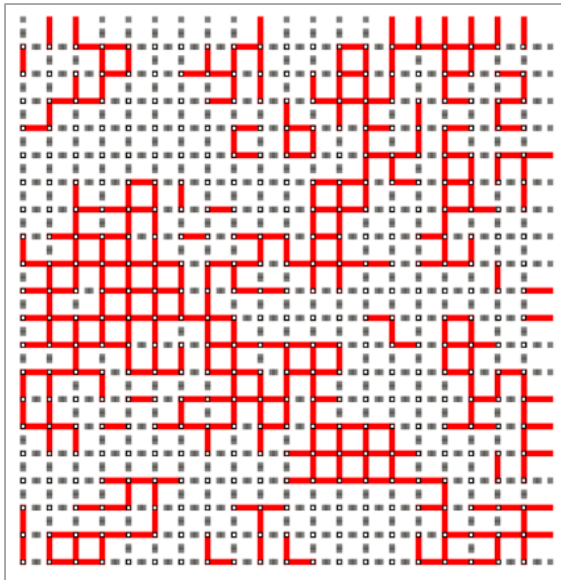


Clusters of occupied links

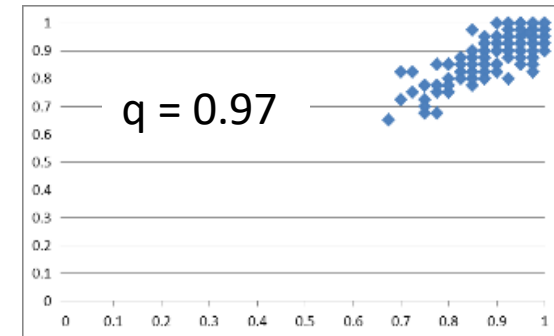
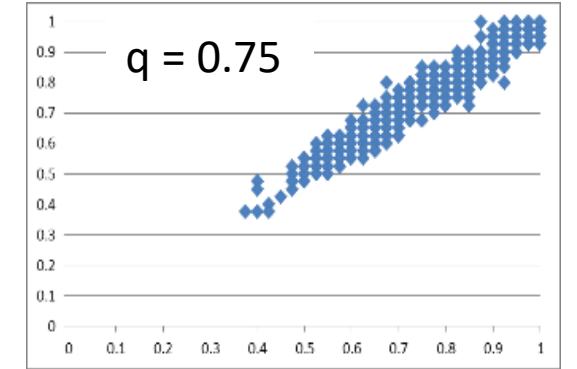
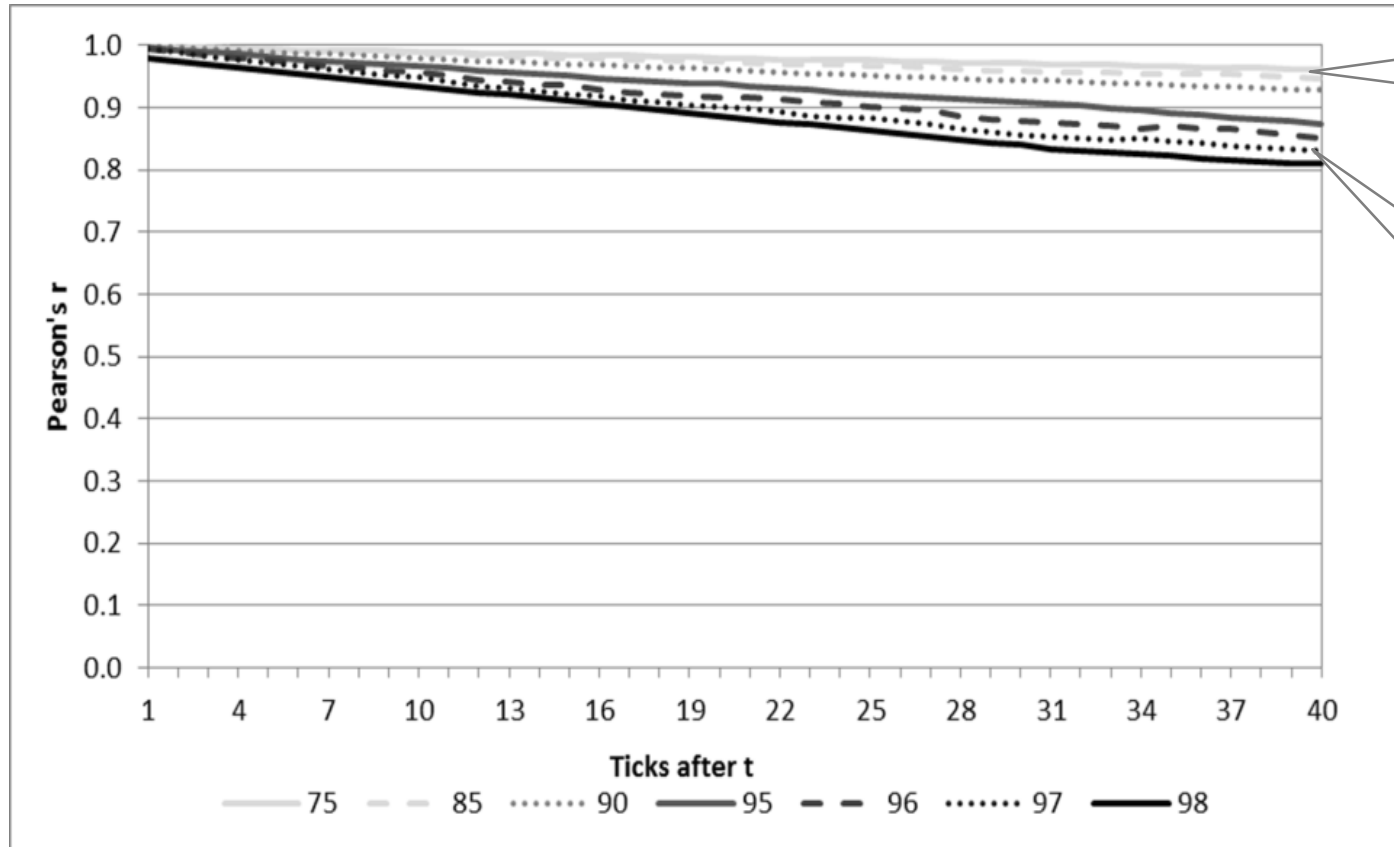
Average occupation rate $q = 0.85$



Average occupation rate $q = 0.95$



Clusters do not change much during driver's search: Autocorrelation of links' occupation



Probability of a parking failure and cruising time curve

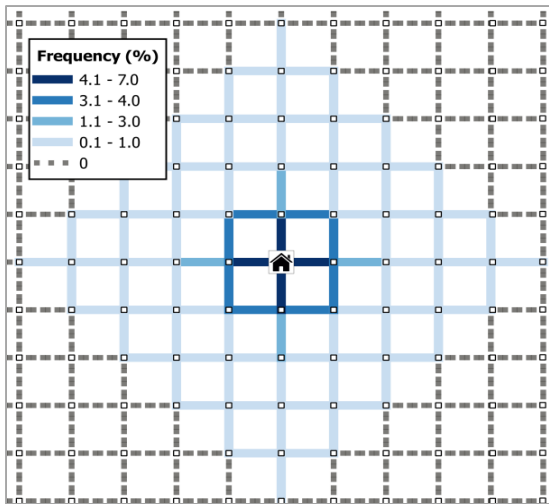
$F_{U(n)}(\tau)$ - wasted search time index

$$F_{U(n)}(\tau) = \sum_{l \in U(n)} \{p_n(l) \mid f_l(\tau) = 0\}$$

$p(\tau, n)$ – probability to cruise for time τ

$$F_{U(n)} = F: p(\tau, n) = (1 - F) * F^\tau$$

$p_n(l)$ fraction of search time wasted while traversing link l
 $f_l(\tau) = 0$ iff l is fully occupied at τ



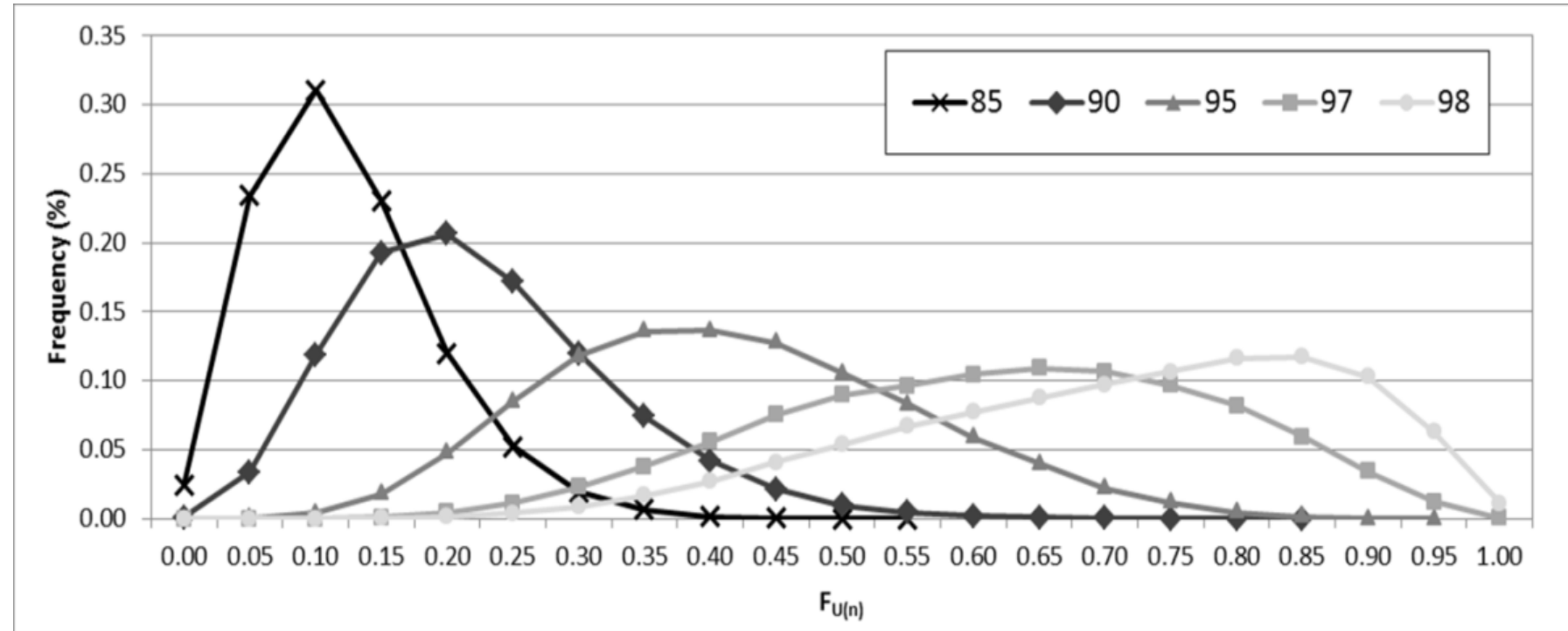
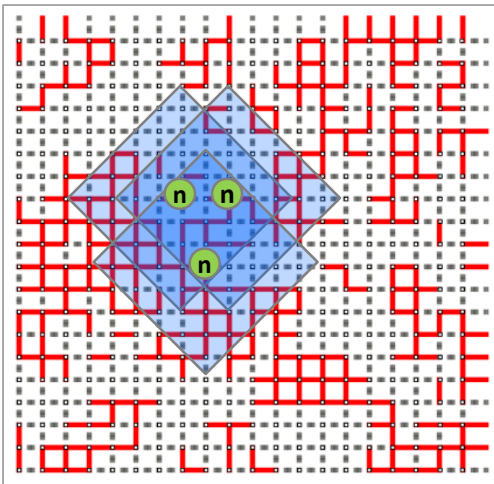
Probability $p_{\text{failure}}(F, \tau)$ of parking failure at τ for $F_{U(n)} = F \pm 0.01$

τ	1	3	5	7	9	Average	STD
F							
0.05	0.05	0.07	0.04	0.05	0.06	0.053	0.0095
0.10	0.09	0.09	0.11	0.11	0.10	0.104	0.0097
0.20	0.20	0.21	0.21	0.20	0.20	0.204	0.0052
0.40	0.39	0.39	0.41	0.42	0.41	0.404	0.0117
0.60	0.59	0.61	0.60	0.60	0.62	0.607	0.0106
0.80	0.81	0.80	0.79	0.82	0.81	0.806	0.0107
0.90	0.90	0.91	0.89	0.91	0.90	0.898	0.0079
0.95	0.96	0.95	0.93	0.96	0.94	0.947	0.0095

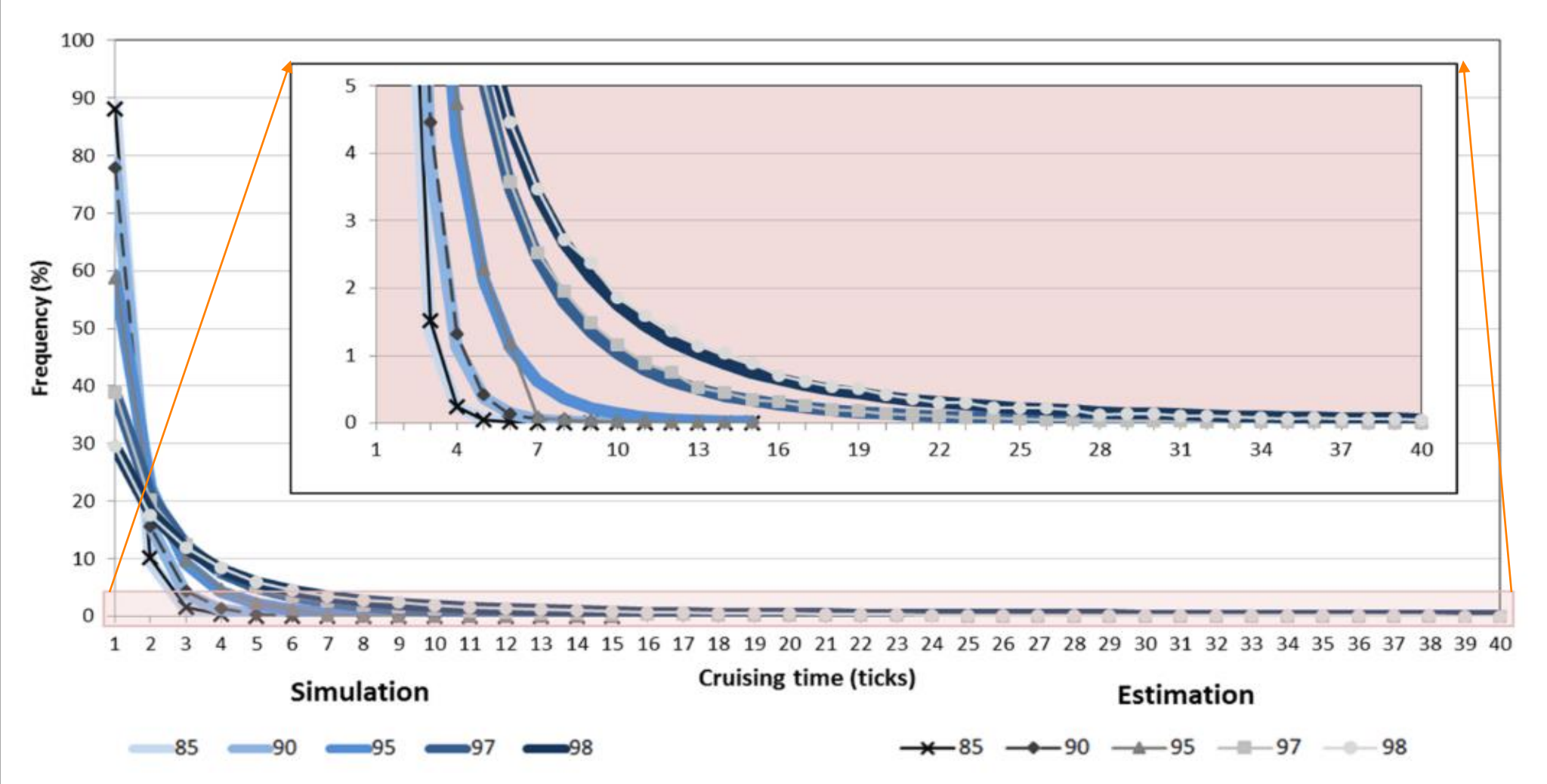
Homogeneous area, average occupation rate q

Let $w_q(F)$ be a fraction of search neighborhoods $U(n)$ with $F_{U(n)} = F$, among search neighborhoods for all destinations n

$$p_q(\tau) = \sum_F \{ (1 - F)^{\tau-1} * w_q(F) \}$$



Simulated vs approximated $p_q(\tau)$, different occupation rates q



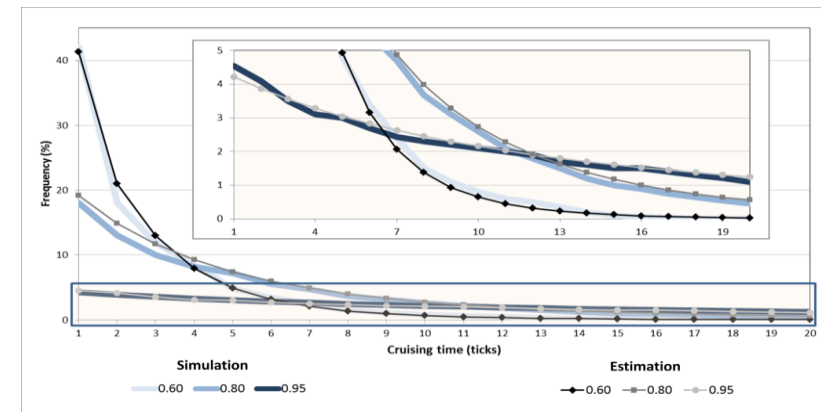
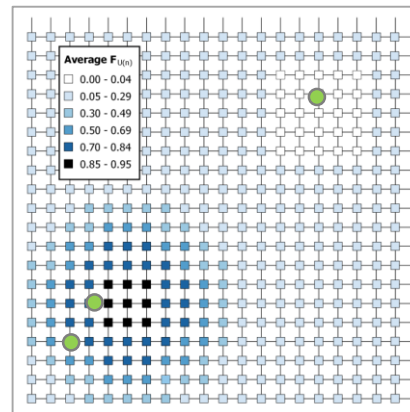
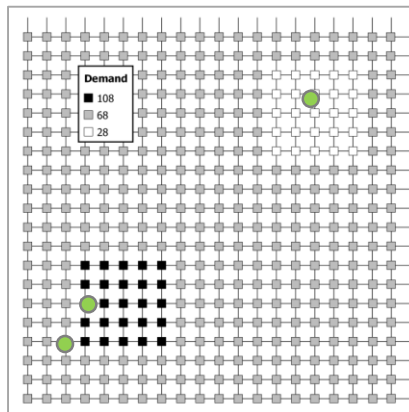
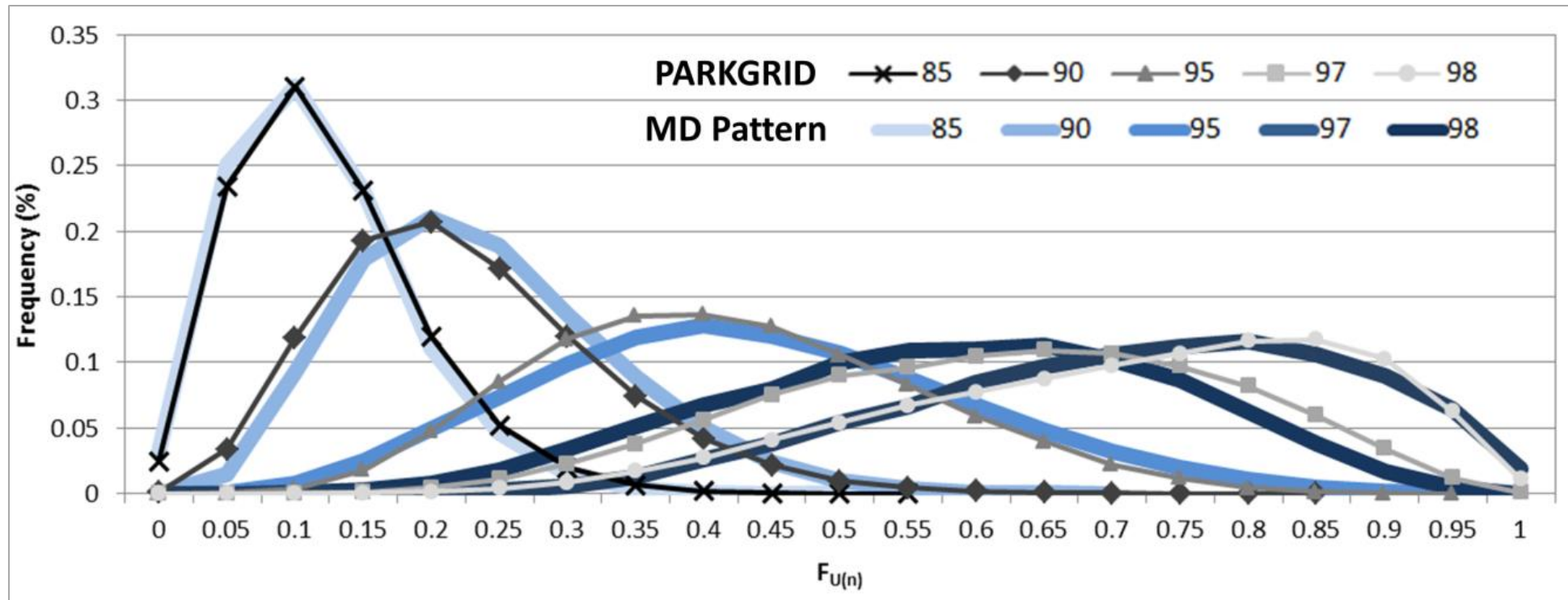
Maximally Dense (MD) parking pattern



*Levy, N., Benenson, I, 2015, *Journal of Transport Geography*, 46, 220–231

CIM CosY Lunch Seminar, 23-Apr-2019, Uppsala University

Approximation of $w_q(F)$ distribution based on the MD pattern



Approximation of $w_q(F)$ distribution based on the MD pattern

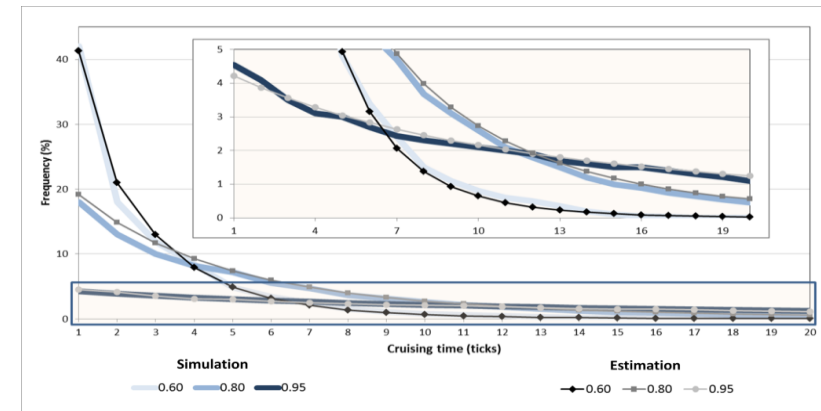
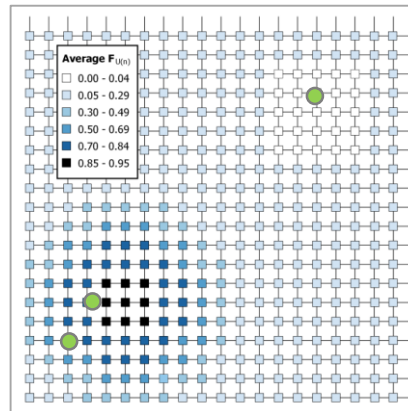
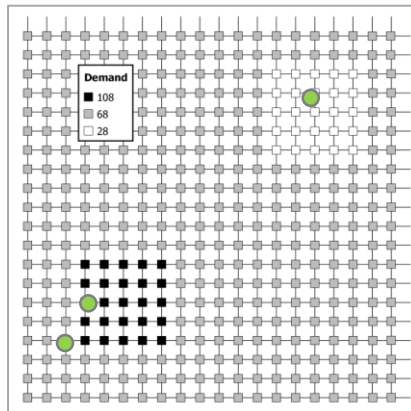
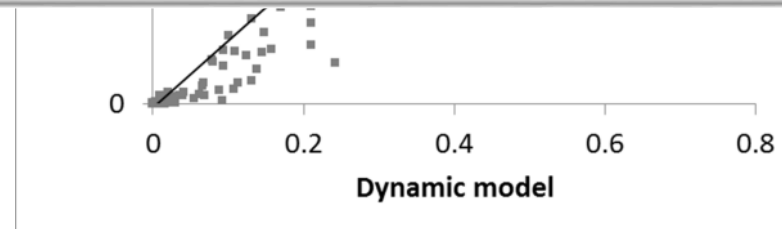
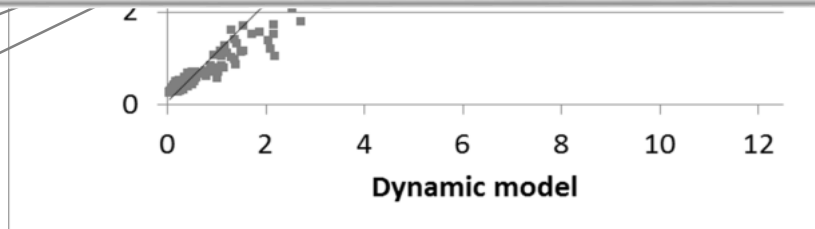
Each point
rep
de



Probability to

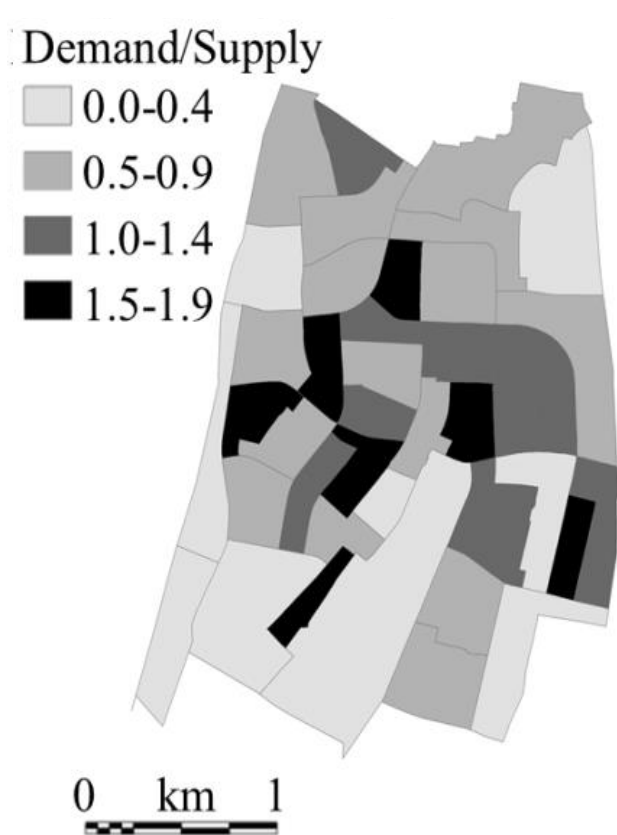
The algorithm of Maximally Dense pattern construction can be turned into a parking reservation system that guarantees zero cruising

Average
search time

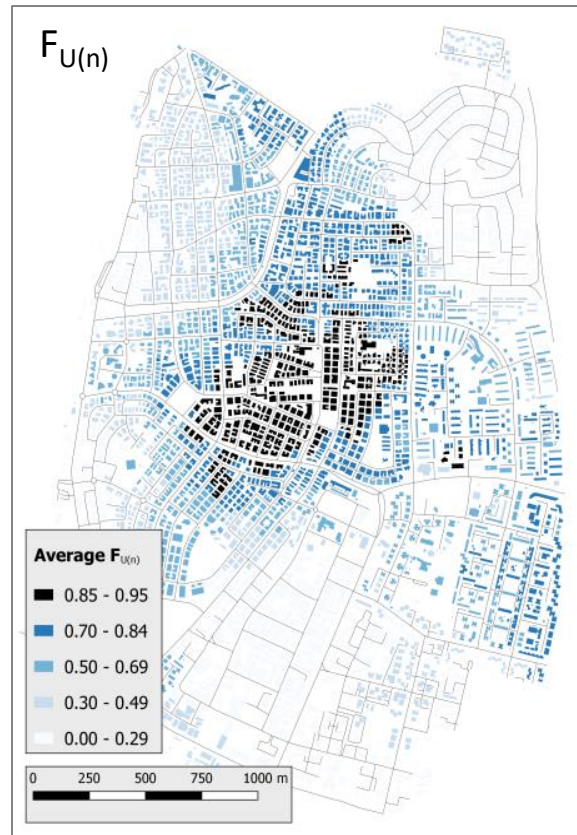


Real example: Bat Yam evening parking

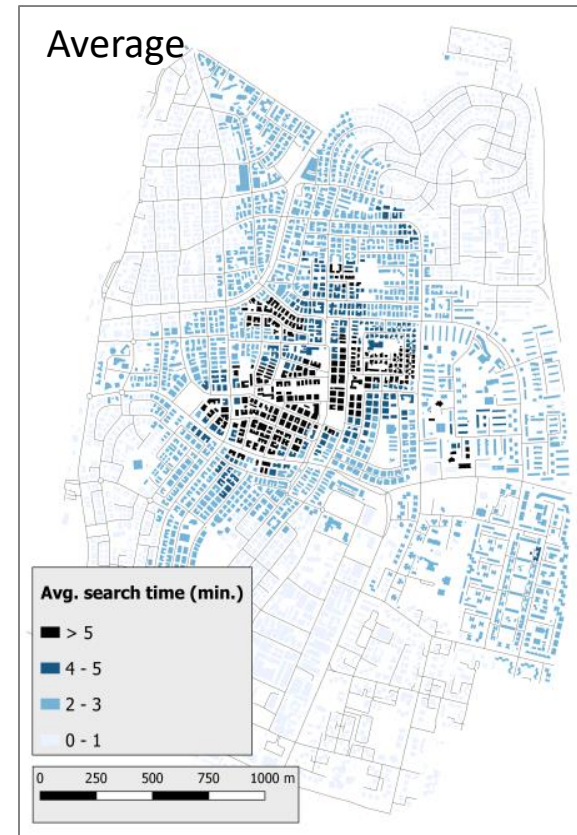
Population 130K pop; Car ownership 35K; 3.3K residential buildings with 51K apts and 17.5K dedicated parking places. Residents park for free on/off-street, visitors parking is paid equally on/off-street. Limited mixed land-uses.



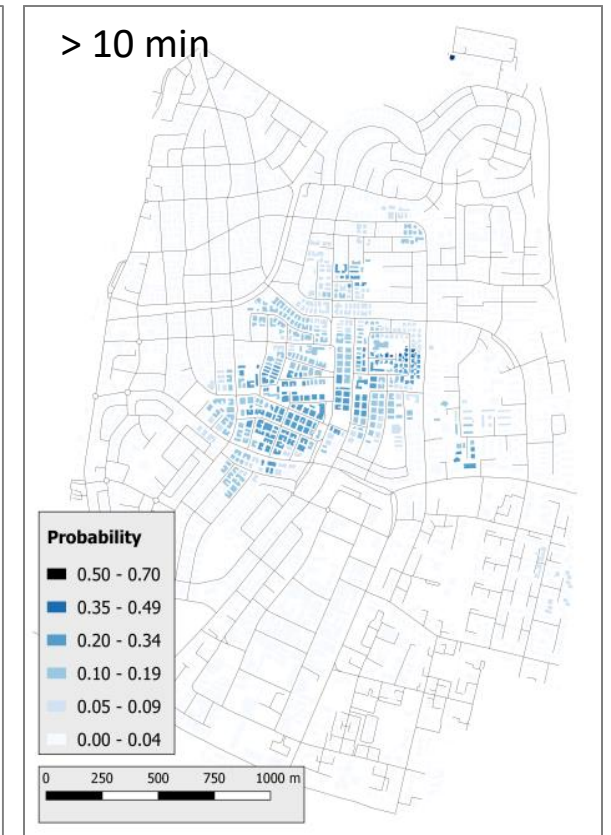
By TAZ, data aggregation



By residents' destinations
(Maximally Dense pattern)



By residents' destinations
(cruising time curve)



By residents' destinations
(cruising time curve)

Parking policy: Recent ideas

Should we adjust parking facilities in the city center to demand?

⁽¹⁾Greg Marsden, The evidence base for parking policies—a review:
The research base, in many instances, does not support, or provides evidence counter to, the assumption that parking restraint makes centers less attractive.
From that on, this claim is reconfirmed many times

How to restrain cruising, then? By increasing parking prices...

⁽²⁾Donald Shoup strongly advocates *adaptive parking prices*, with an objective to preserve 1 per 7 places free. Implemented in a famous San Francisco SF-PARK experiment in 2011-2013, ⁽³⁾Millard-Ball et al, 2014.

What can be positive incentive to change the transportation mode?

Give residents the right to sell their parking permits, ⁽⁴⁾van Ommeren et al, 2014

¹ G Marsden, 2006, Transport Policy 13, 447–457

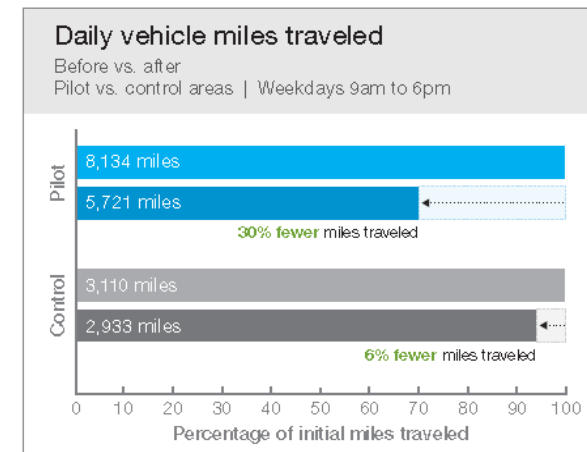
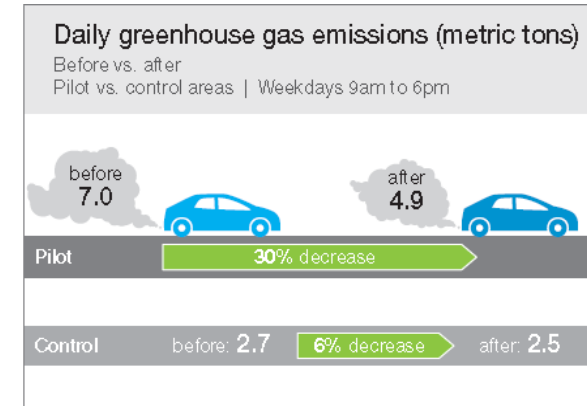
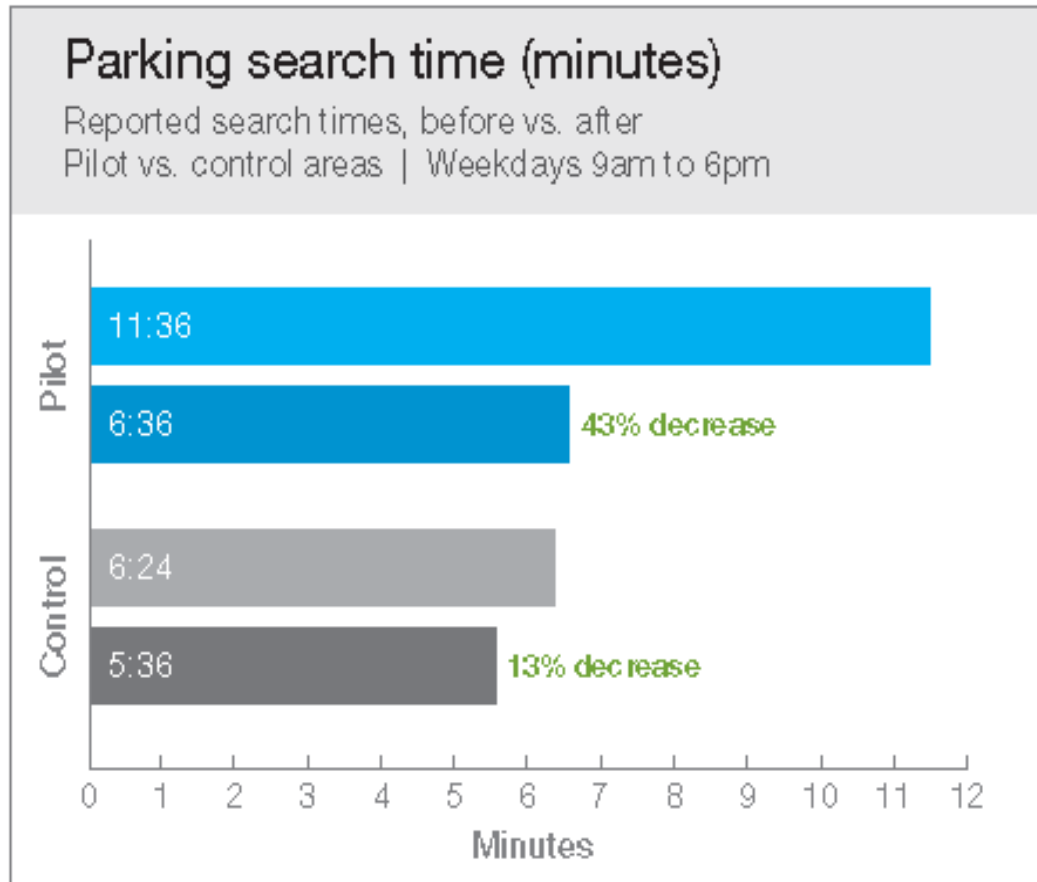
² D. Shoup, 2004, Reg. Sci. Urban Econ. 34 (6), 753–784

³ Millard-Ball et al, 2014 Transportation Research Part A 63, 76–92

⁴ J. van Ommeren et al, 2014, Reg. Sci. Urban Econ. 45 (1) 33–44)

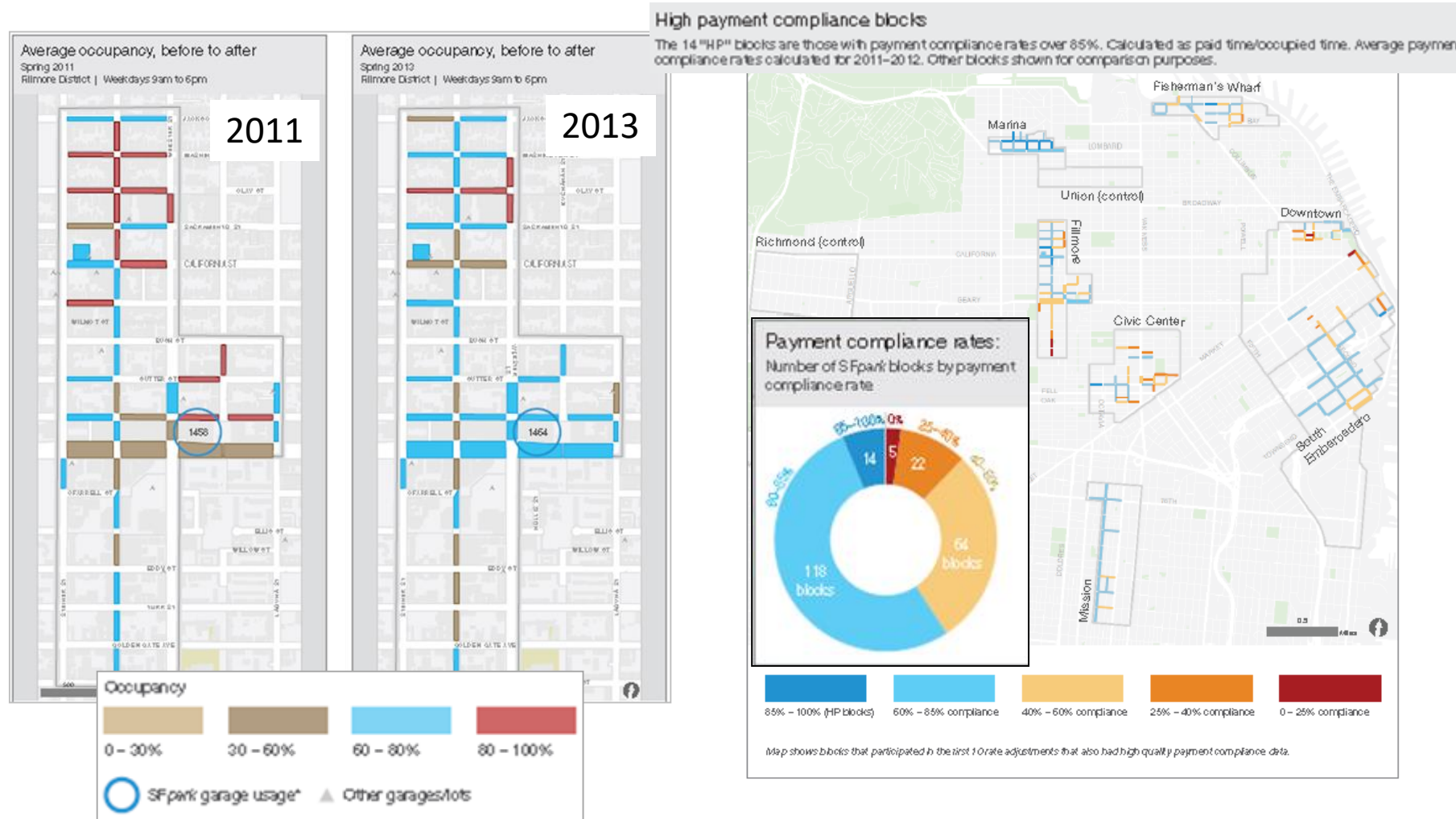
SF-Park: the higher the demand the higher the parking price

Reduced 43% search time, 30% mileage, 30% emissions! But cost **\$18M...**



- Millard-Ball, Adam, Rachel R. Weinberger, and Robert C. Hampshire, *Is the curb 80% full or 20% empty? Assessing the impacts of San Francisco's parking pricing experiment*. *Transportation Research Part A: Policy and Practice* 63 (2014): 76-92.
- SFMTA's evaluation of the SFpark pilot project: http://sfpark.org/resources/docs_pilotevaluation/

Parking is a heterogeneous but “smooth” phenomenon



Occupancy before and after

Readiness to pay is heterogeneous too

Establishing adaptive parking prices

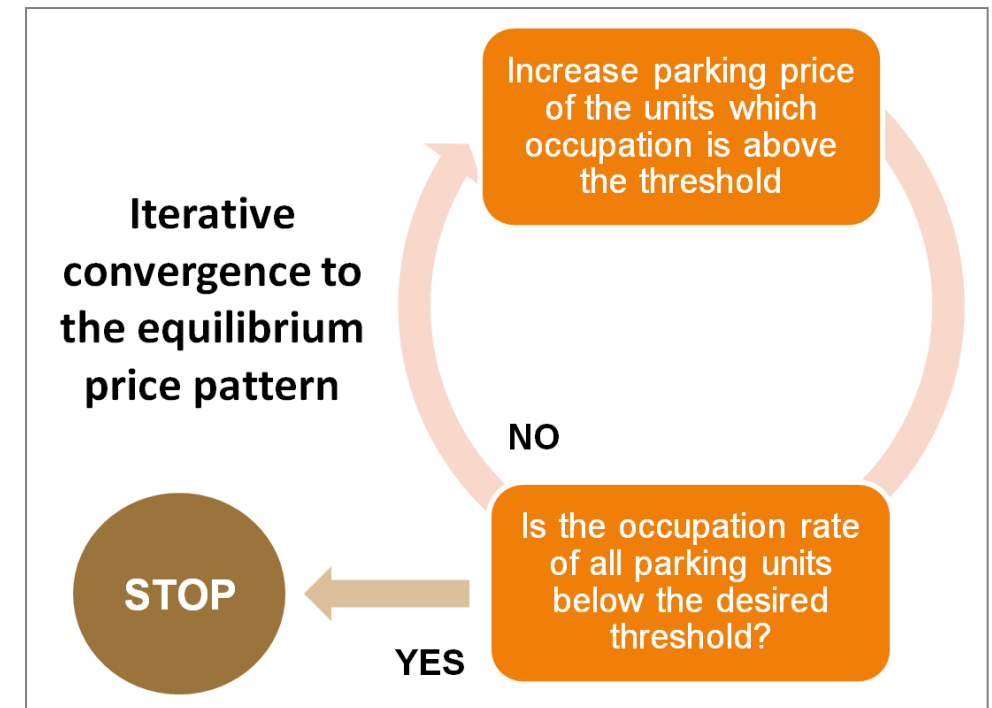
Attractiveness of a spot on a link l at a distance d from driver's c destination (tradeoff between walking distance and willingness to pay):

$$A_l(d) = \min(1, w_c/F_l)/d^a, a < 1$$

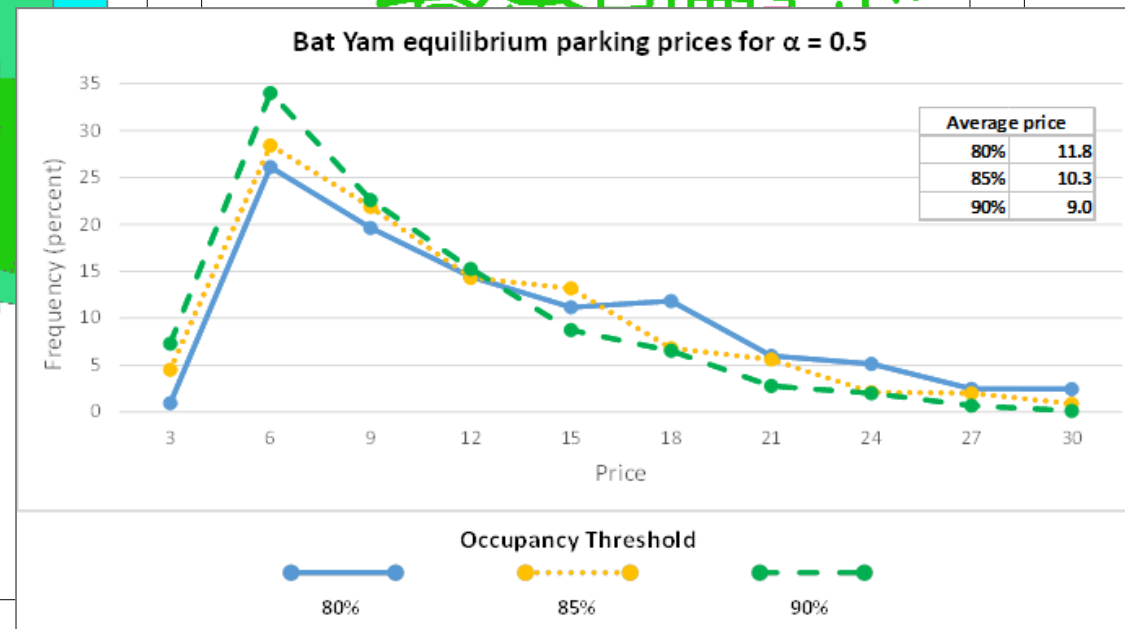
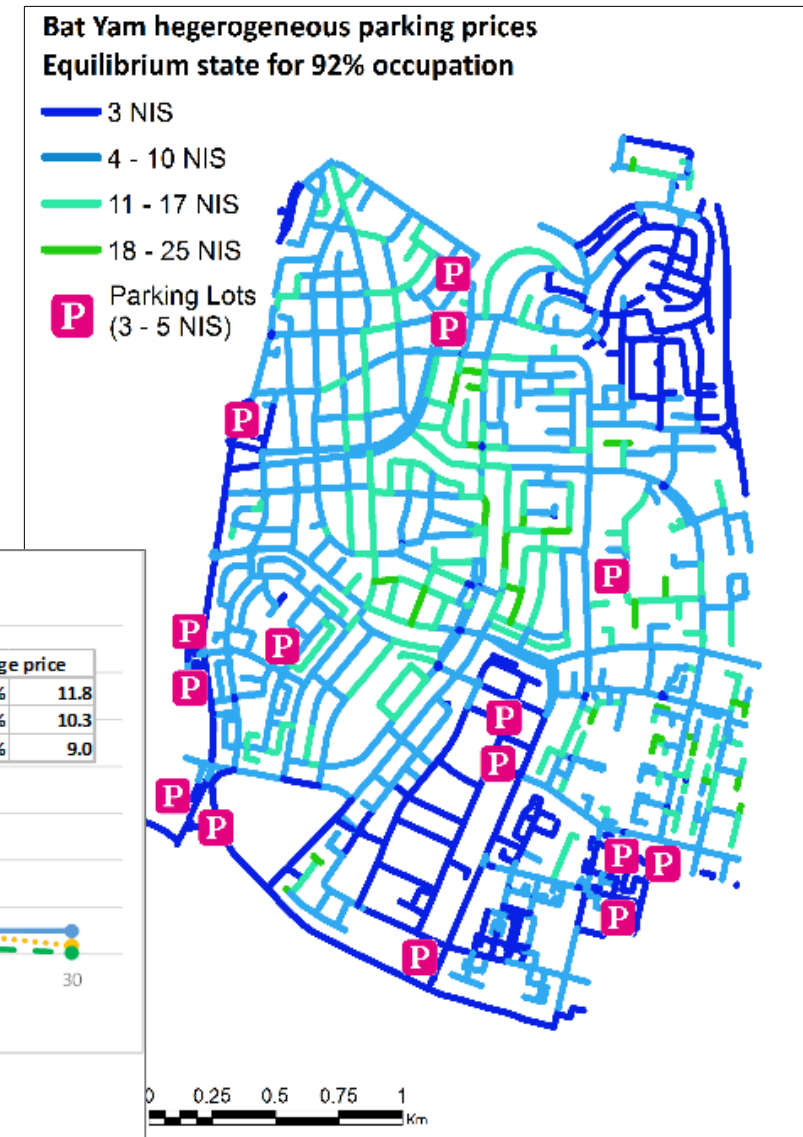
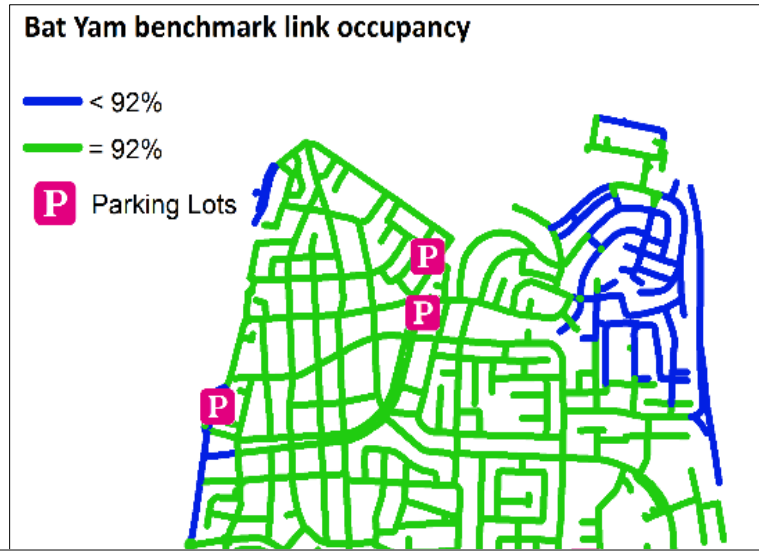
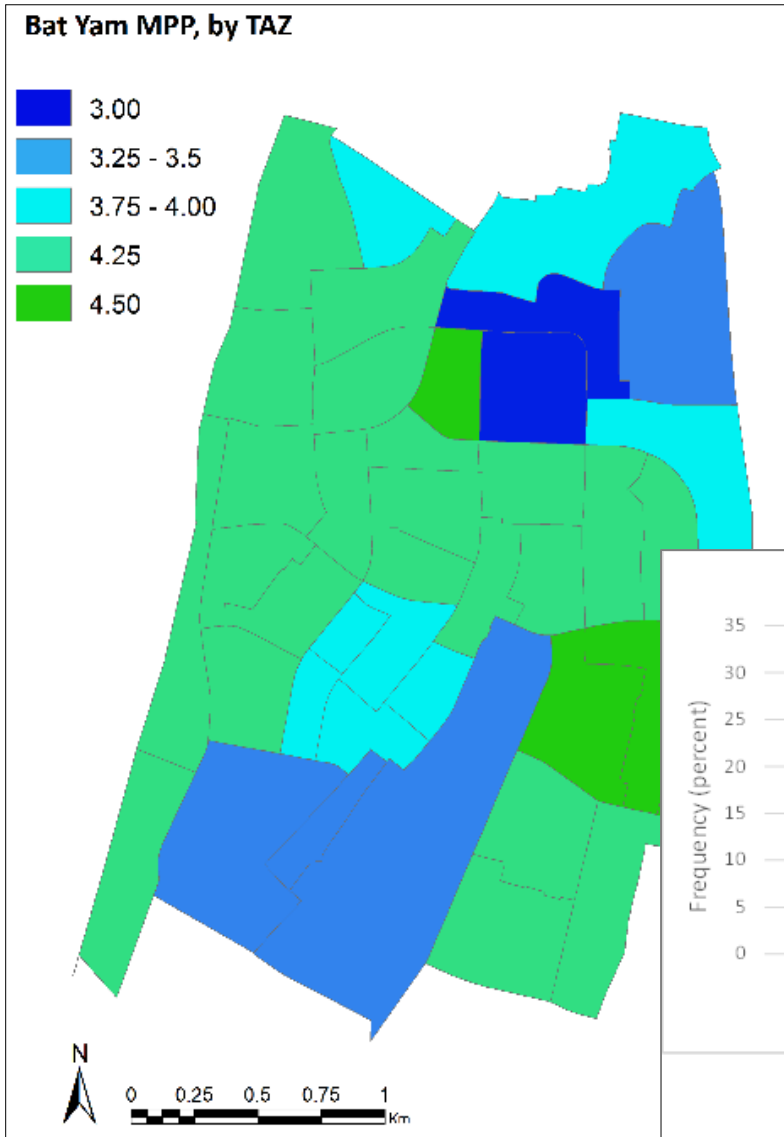
F_l – price of the parking place on l , w_c – minimal perceivable price

If {link l average occupancy $O_l > O_{\text{threshold}}$ }
Then {
 Increase price $F_l = F_l * (1 + x)$
 Reapply MD-pattern construction algorithm
}

*Fulman, Benenson, 2019, Establishing Heterogeneous Parking Prices for Uniform Parking Availability for Autonomous and Human-Driven Vehicles, IEEE ITS Magazine, 11(1), 15 – 28



Adaptive parking prices for Bat Yam



Simple complex problem of urban parking

Conclusions

- Parking patterns of the day/hour are repeated
- Drivers' search behavior is relatively simple and can be revealed in the lab
- Necessary for parking analysis data are readily available: GIS layers of city buildings, streets, parking lots; aggregated statistical data on car ownership
- High-resolution dynamic simulation properly repeats real-world parking patterns
- Parking search time can be estimated with static models, at any level of resolution
- Parking reservation system will guarantee zero cruising
- If reservation is impossible, adaptive parking prices will guarantee zero cruising

What else do we need for establishing urban parking policy?

Anticipating the future...



Thank you!